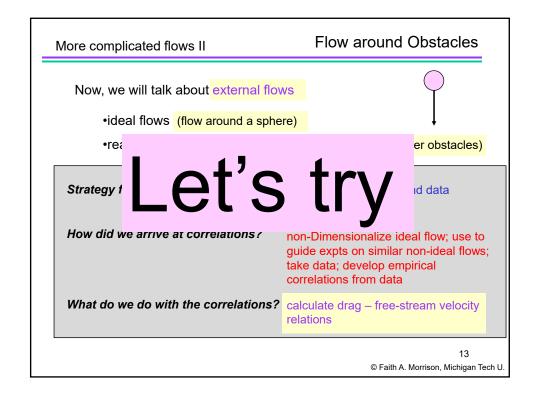
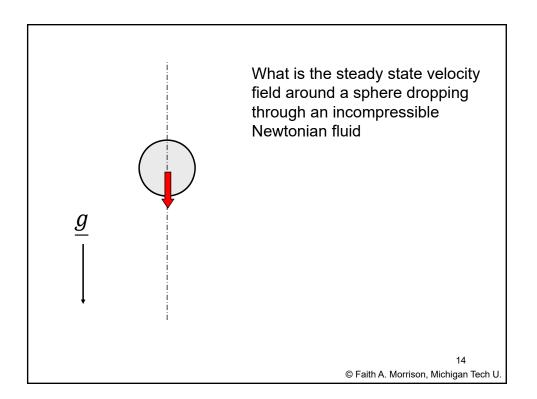
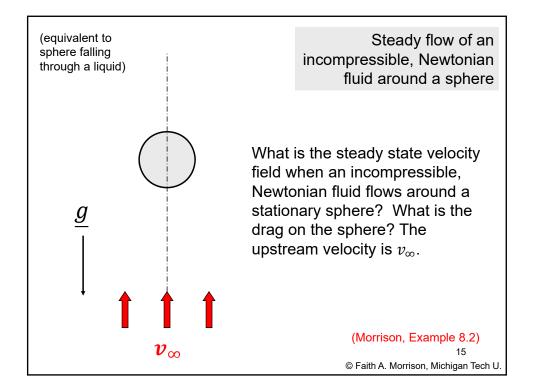
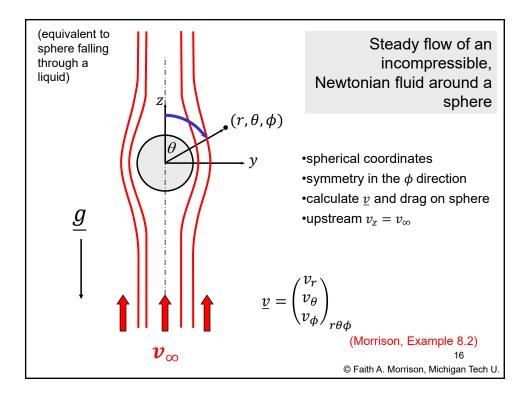


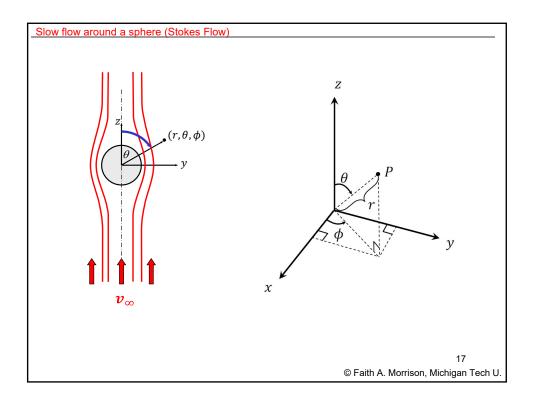
More complicated flows II	Flow around Obstacles
Now, we will talk about external flov	vs
•ideal flows (flow around a sphe	re)
•real flows (turbulent flow around	d a sphere, sky diver, other obstacles)
Strategy for handling real flows:	Dimensional analysis and data correlations
How did we arrive at correlations?	non-Dimensionalize ideal flow; use to guide expts on similar non-ideal flows; take data; develop empirical correlations from data
What do we do with the correlations?	calculate drag – free-stream velocity relations
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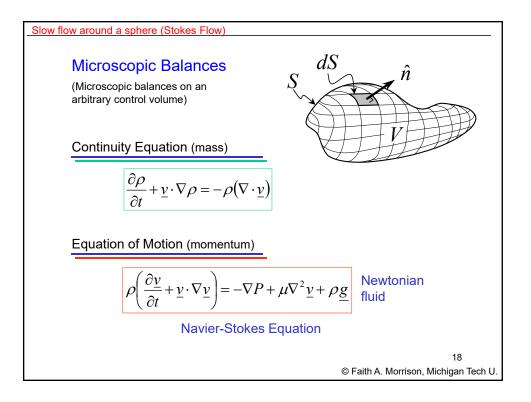




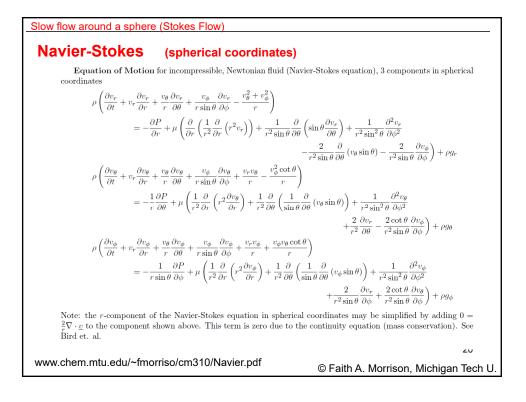


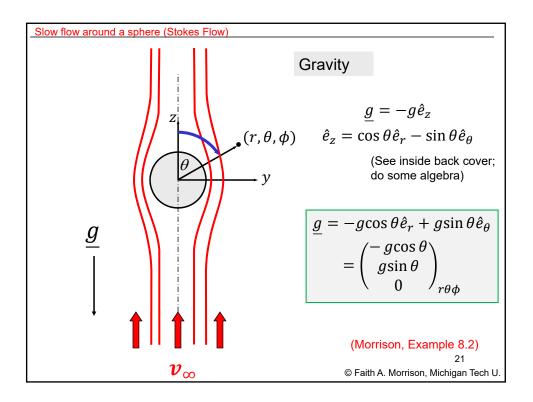


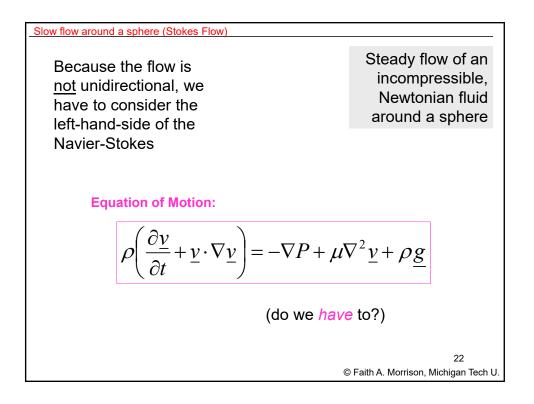




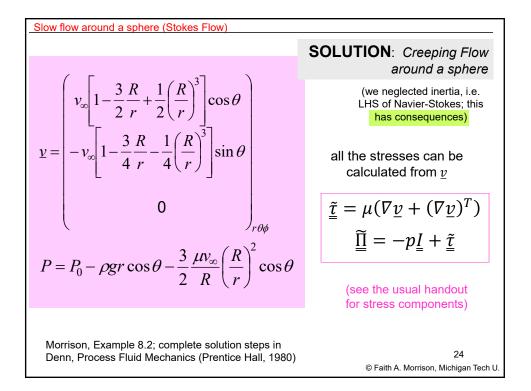
Slow flow around a sphe	ere (Stokes Flow)			
	spherical coordinates)			
The Equation of Continuity and the Equation of Motion in Cartesian, cylindrical, and spherical coordinates				
CM3110 Fall 2011 Faith A. Morrison				
Continuity Equation	n, Cartesian coordinates			
	$rac{\partial ho}{\partial t} + \left(v_x rac{\partial ho}{\partial x} + v_y rac{\partial ho}{\partial y} + v_z rac{\partial ho}{\partial z} ight) + ho \left(rac{\partial v_x}{\partial x} + rac{\partial v_y}{\partial y} + rac{\partial v_z}{\partial z} ight) ~=~ 0$			
Continuity Equation	n, cylindrical coordinates			
	$rac{\partial ho}{\partial t} + rac{1}{r} rac{\partial (ho r v_r)}{\partial r} + rac{1}{r} rac{\partial (ho v_ heta)}{\partial heta} + rac{\partial (ho v_z)}{\partial z} ~=~ 0$			
Continuity Equation	n, spherical coordinates			
	$\frac{\partial \rho}{\partial t} + \frac{1}{r^2} \frac{\partial (\rho r^2 v_r)}{\partial r} + \frac{1}{r \sin \theta} \frac{\partial (\rho v_\theta \sin \theta)}{\partial \theta} + \frac{1}{r \sin \theta} \frac{\partial (\rho v_\phi)}{\partial \phi} = 0$			
	19			
www.chem.mtu.edu/~fm	norriso/cm310/Navier.pdf © Faith A. Morrison, Michigan Tech U			

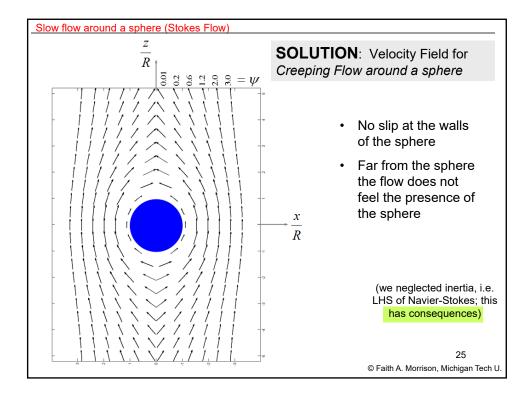


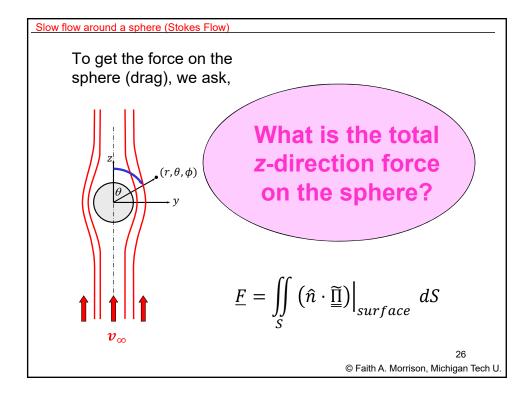


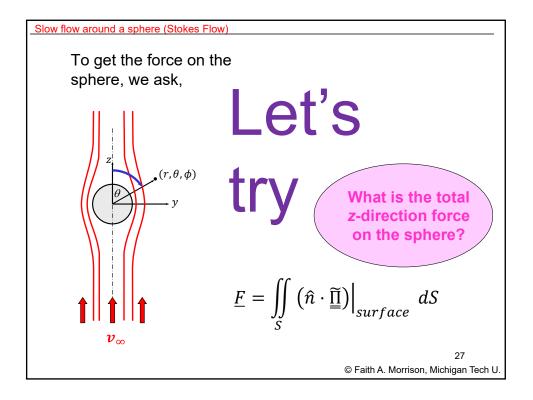


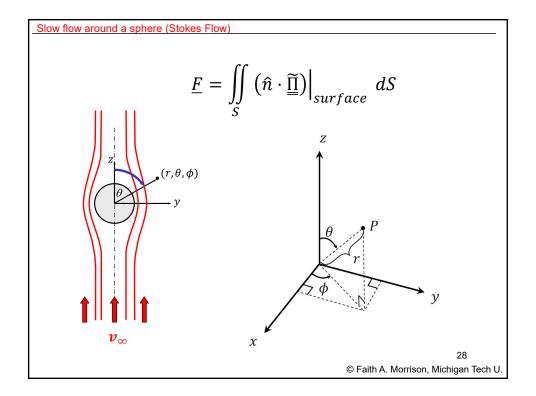
Slow flow around a sphere (Stokes Flow)					
$\underline{v} = \begin{pmatrix} v_r \\ v_\theta \\ v_\phi \end{pmatrix}_{r\theta\phi} \underline{g} = \begin{pmatrix} -g\cos\theta \\ g\sin\theta \\ 0 \end{pmatrix}_{r\theta\phi} p = p(r)$	c, θ) Steady flow of an incompressible, Newtonian fluid around a sphere				
Eqn of Continuity: $\left(\frac{1}{r^2}\frac{\partial(r^2v_r)}{\partial r} + \frac{1}{r\sin\theta}\frac{\partial v_\theta\sin\theta}{\partial\theta}\right) = 0$ Creeping Flo					
Eqn of $\rho \left(\frac{\partial \mu}{\partial t} + \underline{v} \cdot \nabla \underline{v} \right) = -\nabla P + \mu \nabla^2 \underline{v} + \rho \underline{g}$ Motion: steady neglect state inertia					
BC1: no slip at sphere surface BC2: velocity goes to v_{∞} far from sphere					
23					
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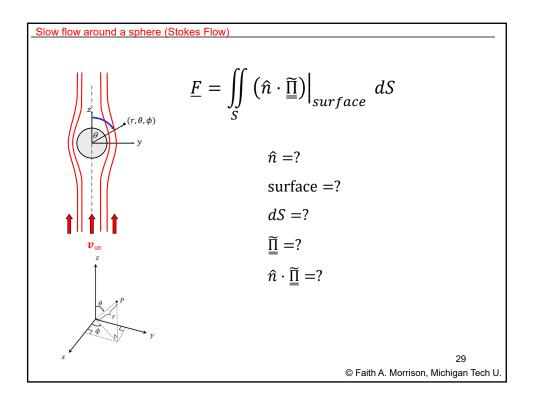


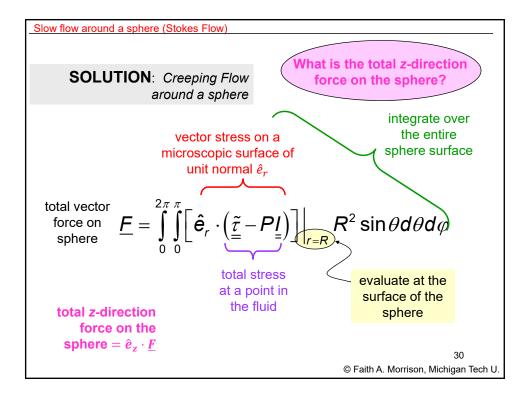


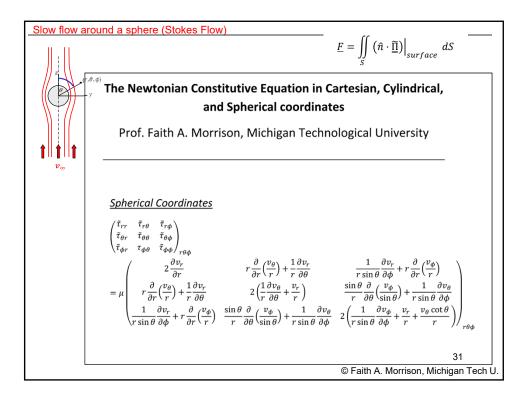


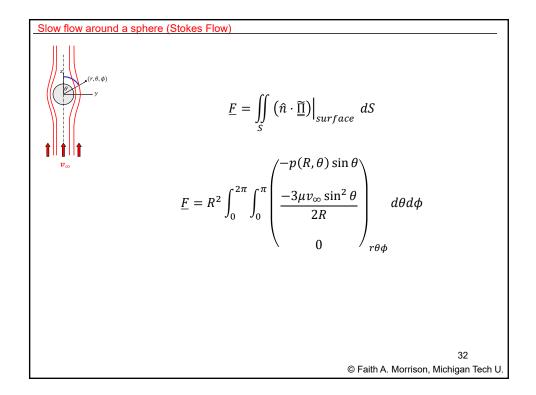


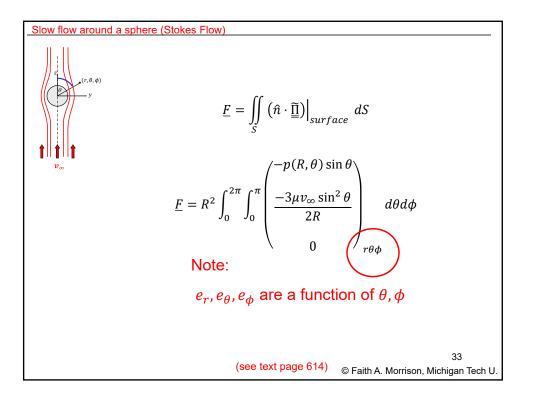


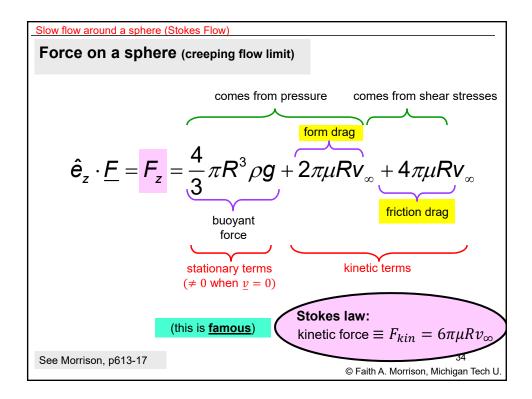


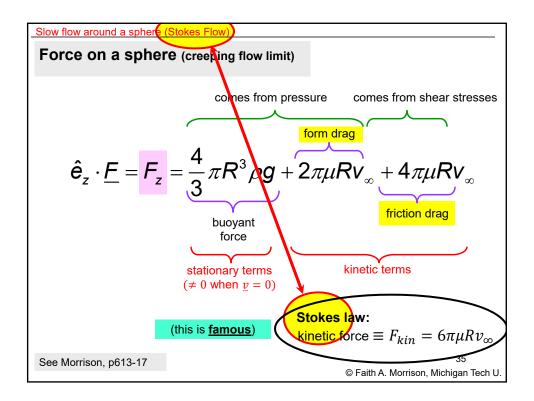


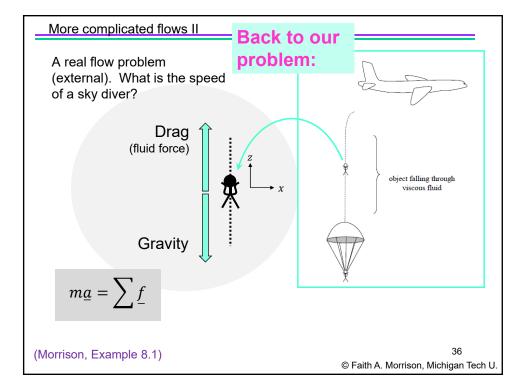


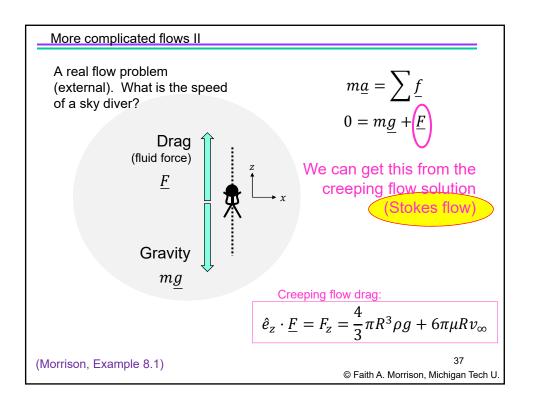


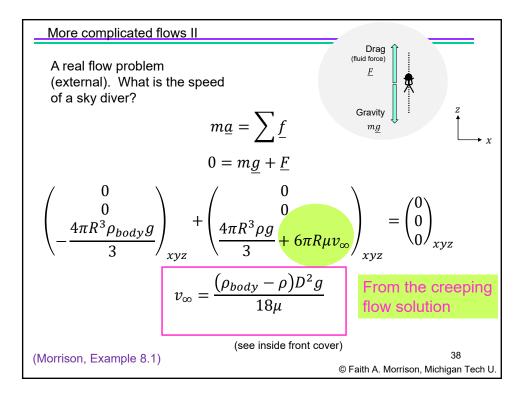


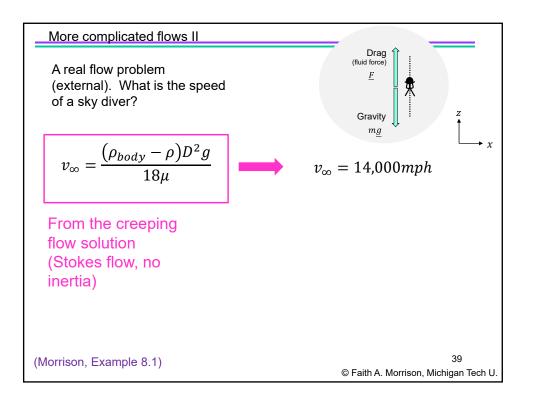


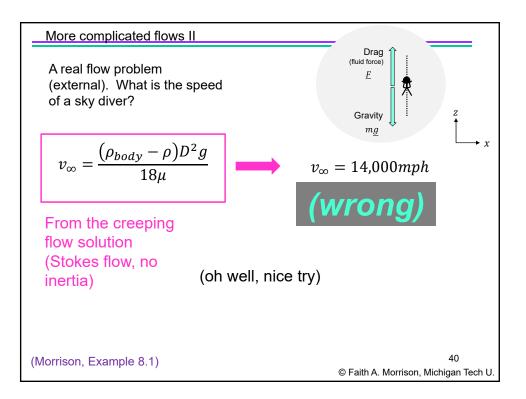


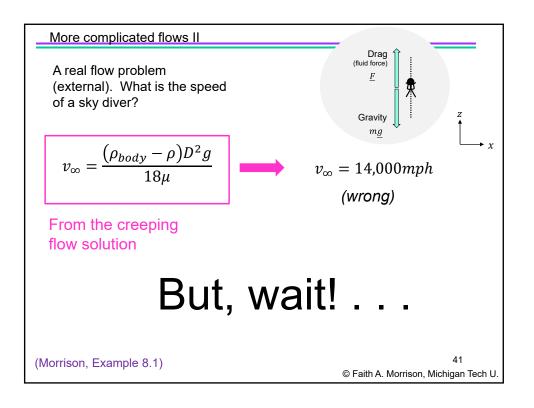


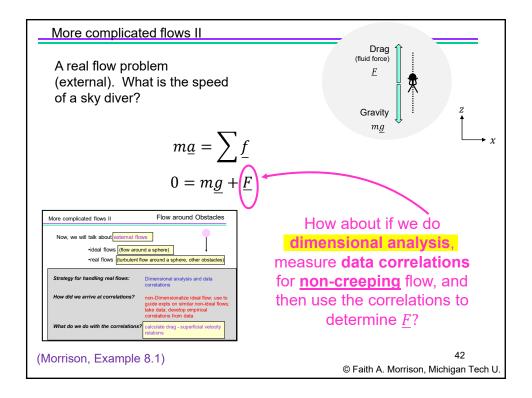


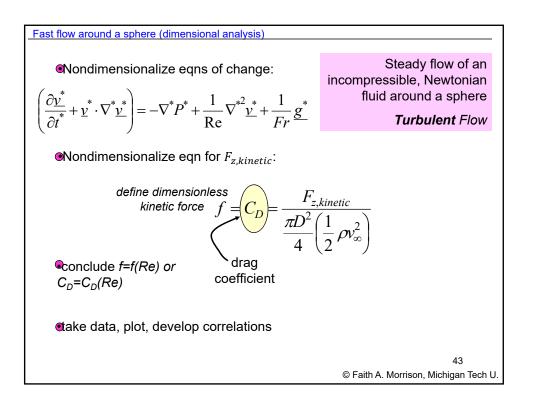


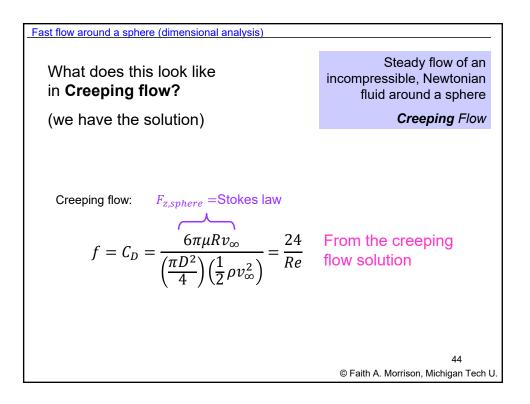


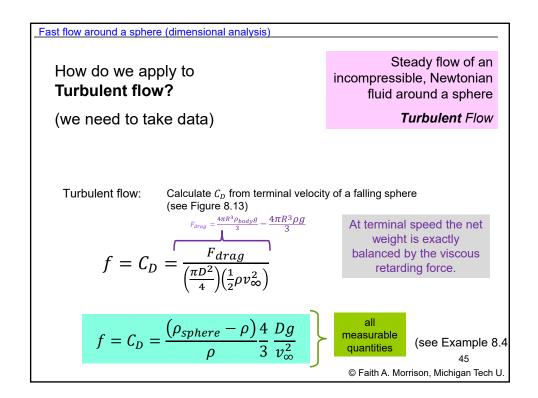


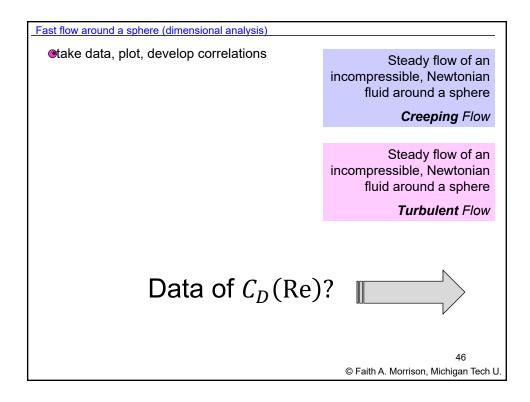


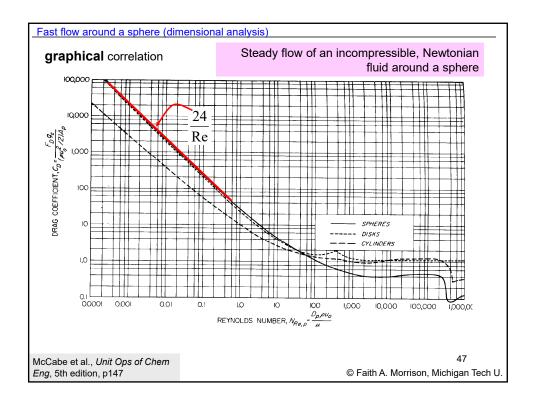


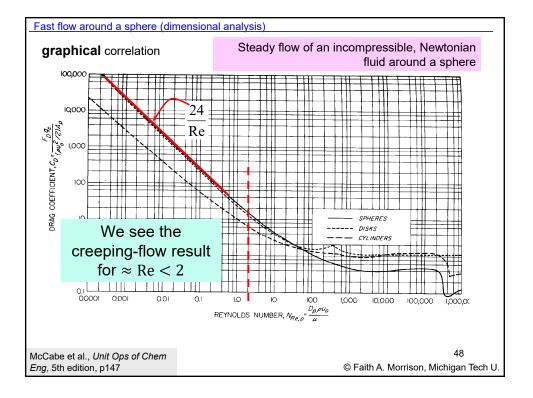












Fast flow around a sphere (dimensional analysis)						
correlation equations	Steady f	ow of an incom	npressible, N fluid around			
creeping $f =$	110	<i>Re</i> < 0				
vortices $f = 18.5$ wake flow $f = 0$		$2 \le Re \le 500 \le Re \le 500$	_	BSL, p194		
Ouse correlations in enginee •particle settling	ring practice		opp Dird of			
•particle settling •entrained droplets in distillation columns •particle separators						
 drop coalescence 						
Dr. Morrison developed a single, combined correlation						
Denn, Process Fluid Mechanics, 1980 Bird, Stewart, Lightfoot, Transport Phenomena, 19	960 and 2006	© Faith A. Morrison, Michigan Tech U.				

