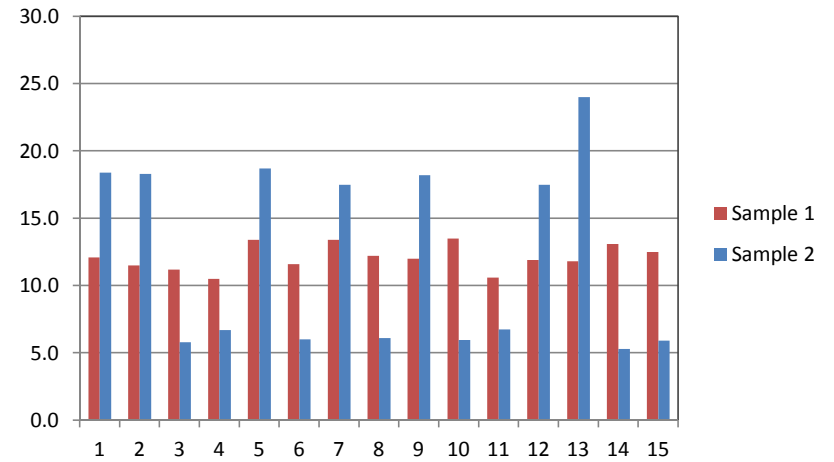


sample 1			sample 2		
1	12.1	12.09 mean	1	18.4	12.07 mean
2	11.5	0.96 std dev	2	18.3	6.82
3	11.2	0.25 std error	3	5.8	1.76 std error
4	10.5	2.14 t_.975	4	6.7	2.14 t_.975
5	13.4	11.56 t_a	5	18.7	8.29 t_a
6	11.6	12.62 t_b	6	6.0	15.85 t_b
7	13.4	12 target value	7	17.5	12 target value
8	12.2	-0.350 t	8	6.1	-0.042 t
9	12.0	37%	9	18.2	48%
10	13.5	63%	10	6.0	52%
11	10.6		11	6.8	
12	11.9		12	17.5	
13	11.8		13	24.0	
14	13.1		14	5.3	
15	12.5		15	5.9	

The true mean of the population is between t\_a and t\_b with 95% confidence.

What is the probability that the true mean is less than 12oz?

What is the probability that the true mean is greater than 12oz?



(Finite sample size)

**EXAMPLE 3.1** Based on the seven data points we have on Blue Fluid 175 density, what is the probability that the true density of Blue Fluid 175 is less than 1.75 g/cm<sup>3</sup>?

$$\Pr(\bar{\rho} \leq b) = \Pr\left(t \leq \left[t_b = \frac{b - \bar{\rho}}{s / \sqrt{n}}\right]\right)$$

$$= T\left(\frac{b - \bar{\rho}}{s / \sqrt{n}}\right)$$

In Excel:

$$T(t) = \begin{cases} t < 0 & TDIST(-t, v, 1) \\ t \geq 0 & 1 - TDIST(t, v, 1) \end{cases}$$

i	X <sub>i</sub>	(X <sub>i</sub> - mean) <sup>2</sup>
1	1.7348	3.26E-04
2	1.7465	4.03E-05
3	1.7359	2.87E-04
4	1.83	5.95E-03
5	1.74688	3.56E-05
6	1.74412	7.62E-05
7	1.73173	4.46E-04
sample mean=	1.752847	
sample std dev=	0.034553	

b = 1.75  
t<sub>b</sub> = -.22  
T(t<sub>b</sub>) = TDIST(0.22, 6, 1) = 0.416583

**Answer: 42%**

(assuming normal distribution we calculated 41%)

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