

CM4650 Polymer Rheology
Prof. Faith Morrison

Material Behavior Outline

16 March 2015

1. Steady Shear
 - a. Linear Polymers
 - i. Versus shear rate
 - ii. As a function of Molecular weight
 - iii. As a function of molecular weight distribution
 - b. Linear Polymers with solid filler
 - i. Versus shear rate
2. Unsteady Shear (or Elongation) (small strain)
 - a. Linear Polymers
 - i. Versus frequency
 - ii. Cox-Merz rule
 - b. Other architectures
3. Effect of temperature
4. Unsteady Shear (large strain)
 - a. Start-up
 - b. Cessation
 - c. Step Strain
5. Steady Elongation
6. Unsteady Elongation (large strain)

Experimental Data

Chapter 6

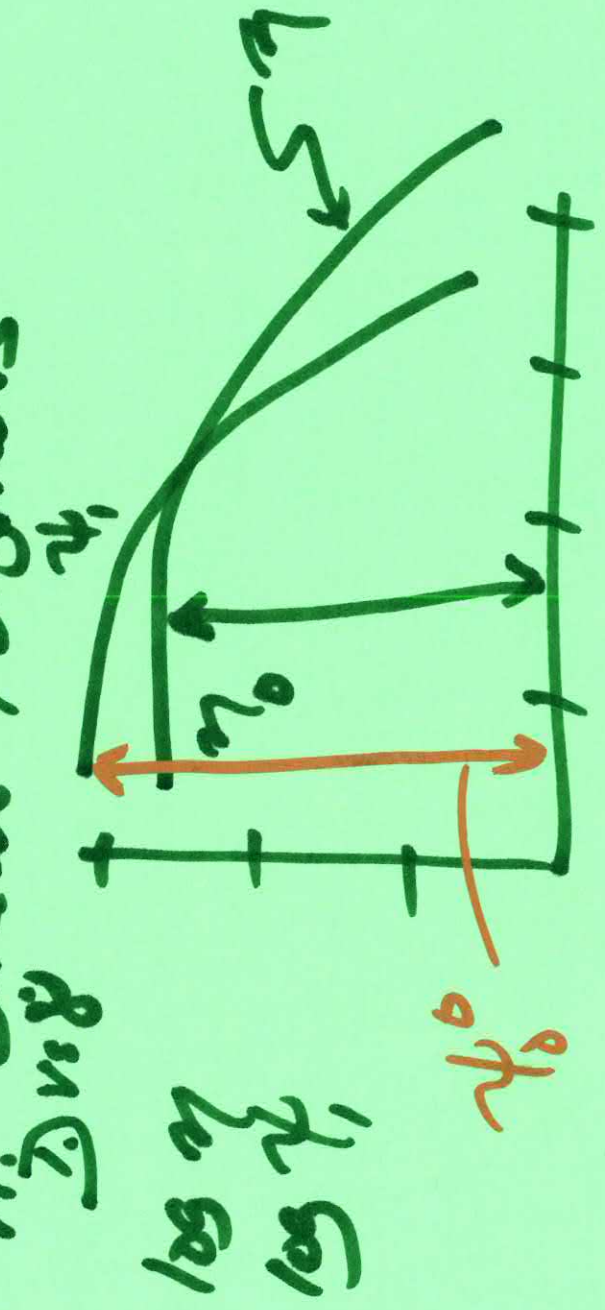
①

$$\dot{\gamma}(A) = \dot{\gamma}_0$$

$$\eta, \psi_1, \psi_2$$

I. Steady Shear

A. Linear Polymers



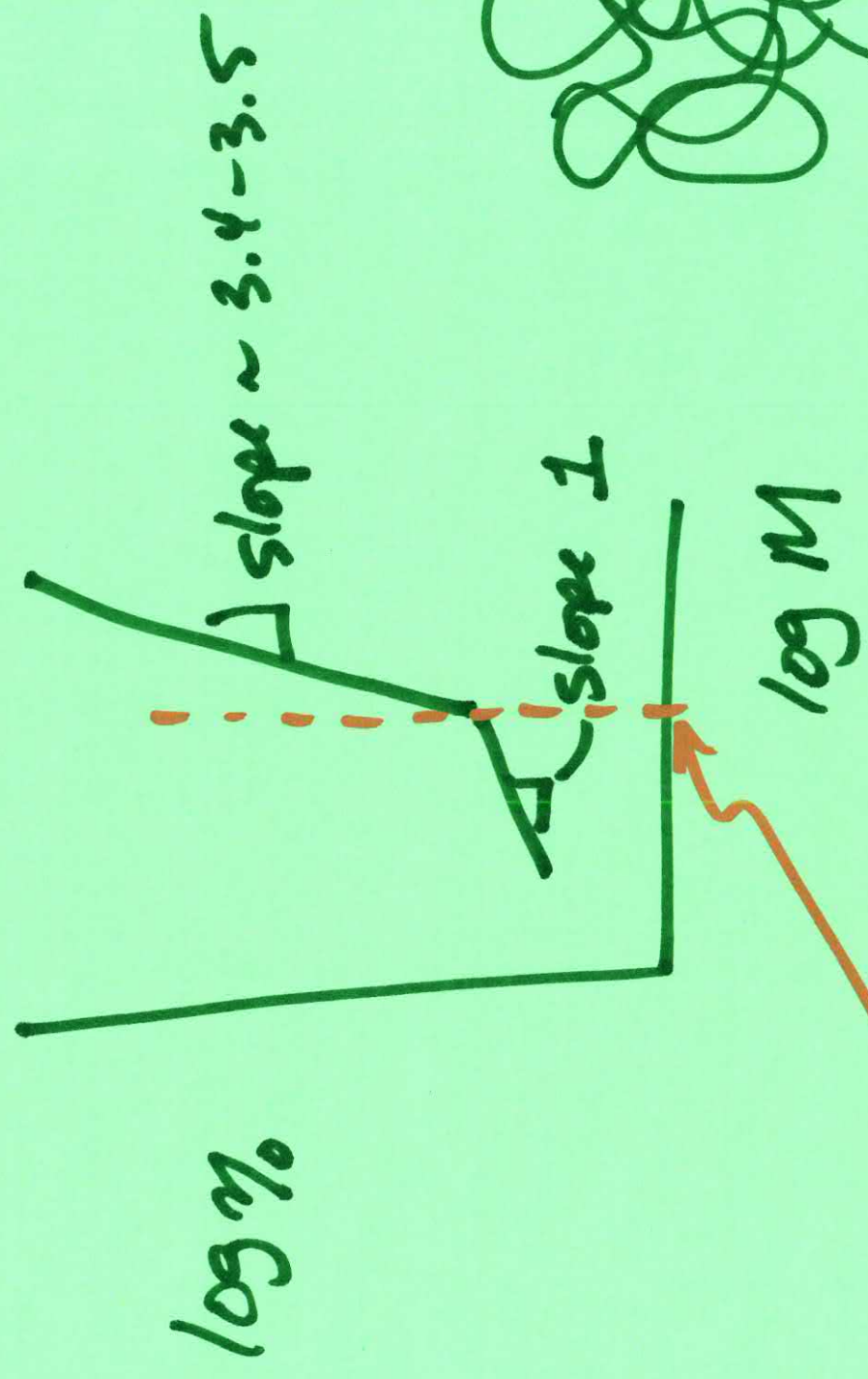
$\log \dot{\gamma}$

$$\lim_{\dot{\gamma} \rightarrow 0} \eta = \eta_0 = \text{zero shear viscosity}$$

$$\psi_0 = \text{zero shear 1st normal coef}$$

②

② η as a function of M :



M_c
critical MW for
entanglement

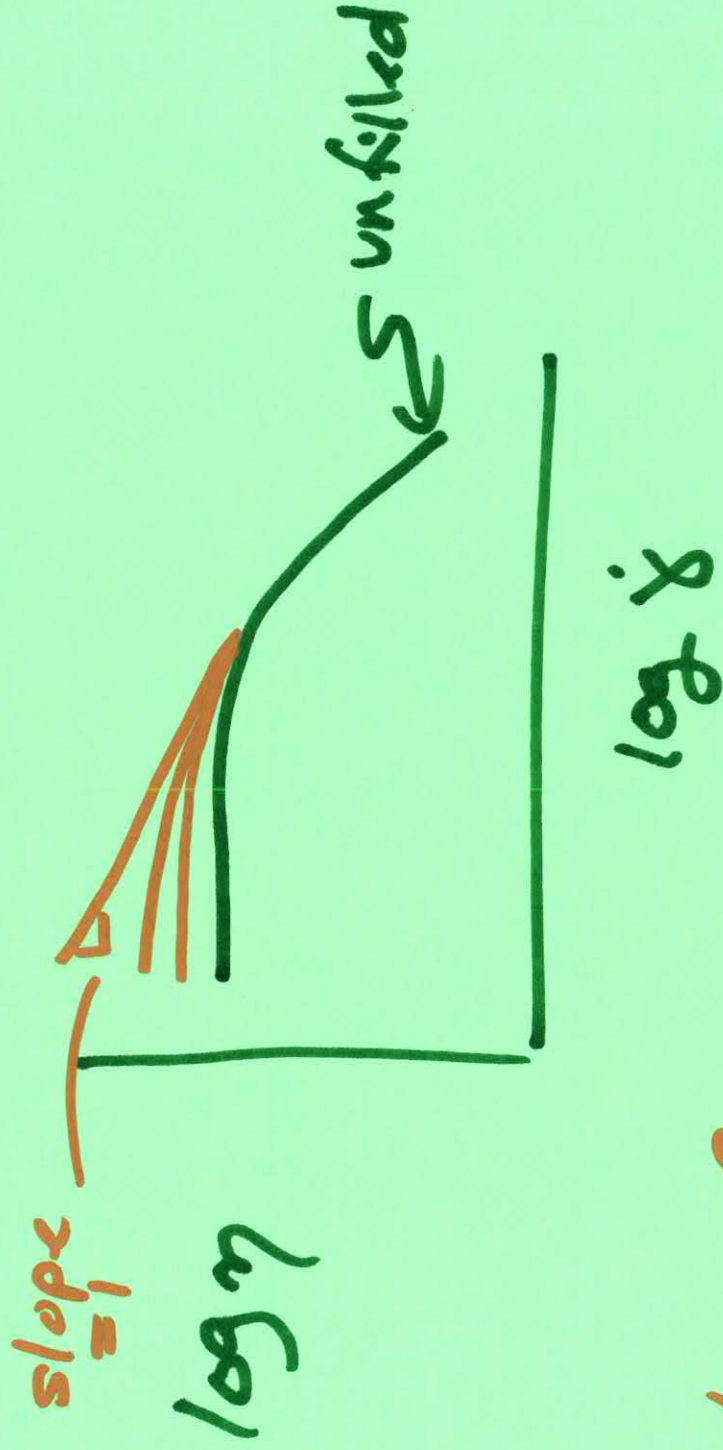
$M > M_c$
Polymers are
entangled.

③ $\eta(\delta)$ as a function of Molecular Wt Dist (MWD)



B) Linear Polymers + solid filler

1) vs shear rate, $\dot{\gamma}$



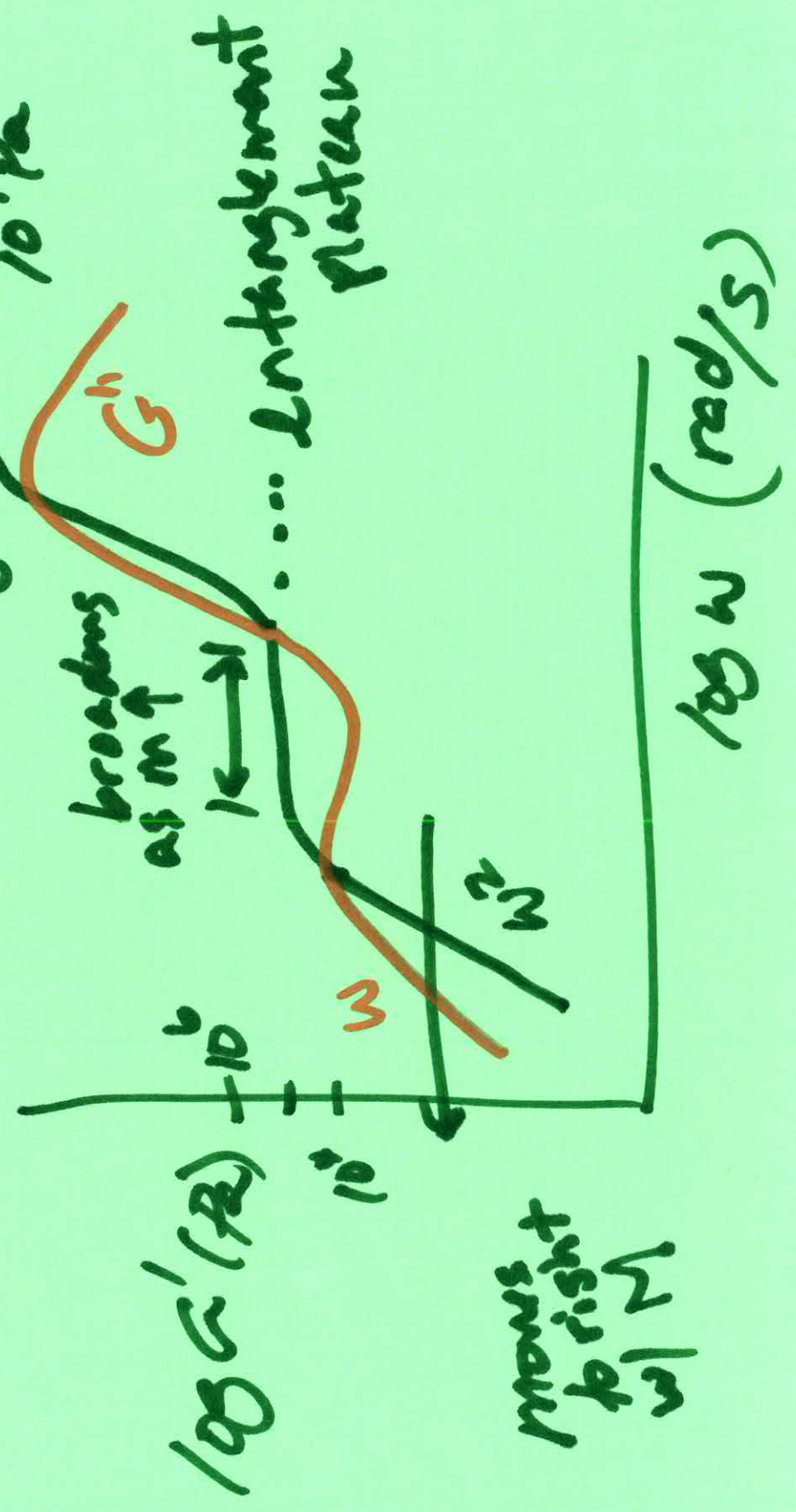
slope of 1
at low $\dot{\gamma} \Rightarrow$ yield stress

⑤

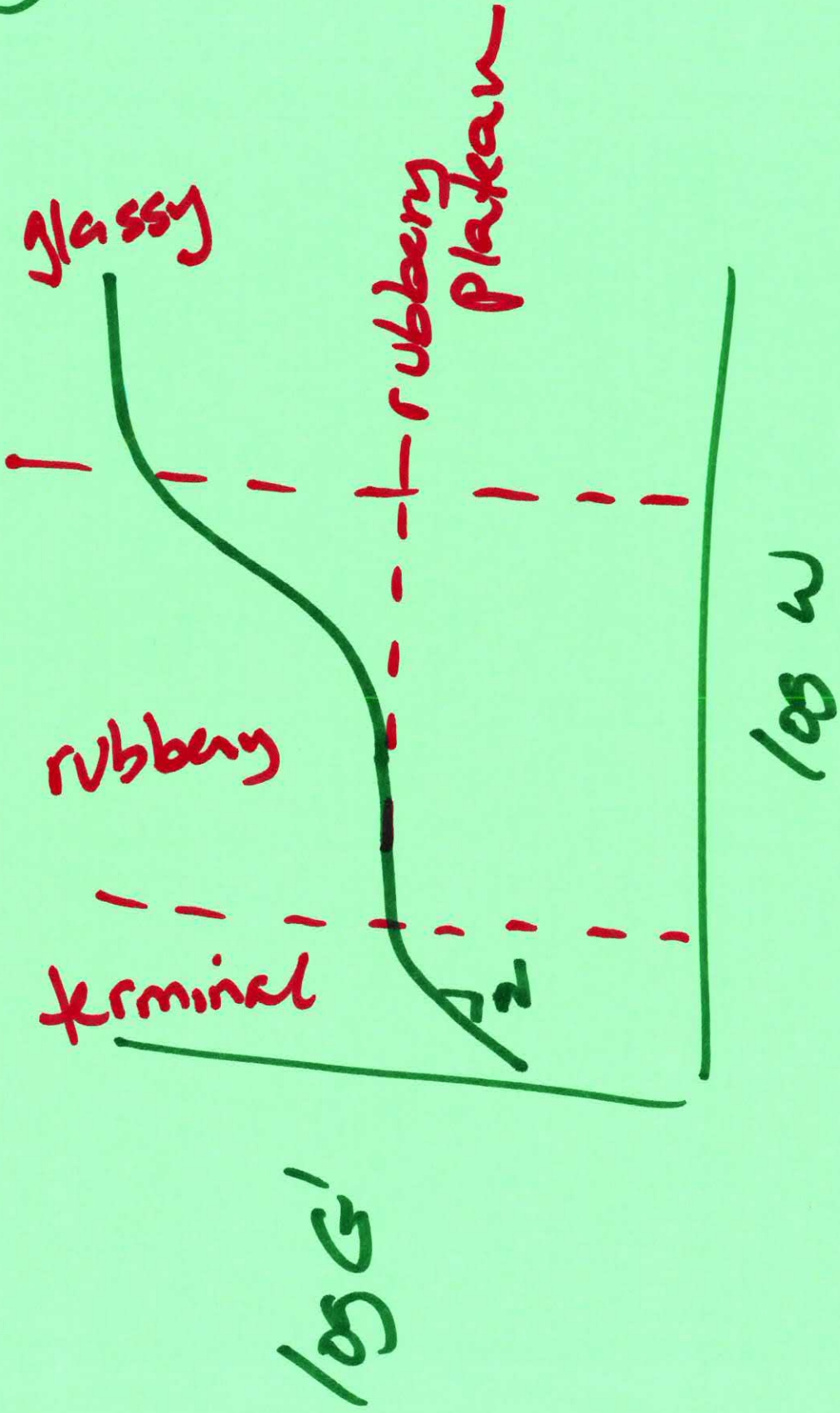
Unsteady Shear (or Elongation) SAOS (small strain)

A. Linear Polymers

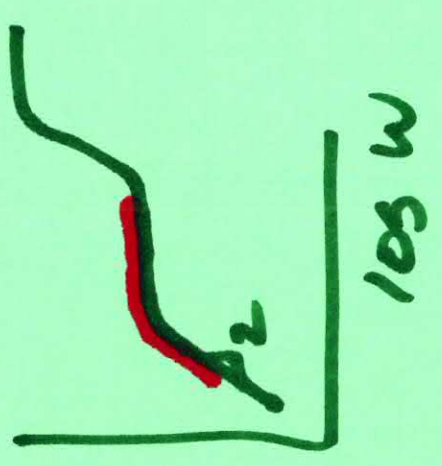
1. Versus ω (frequency)



5.5

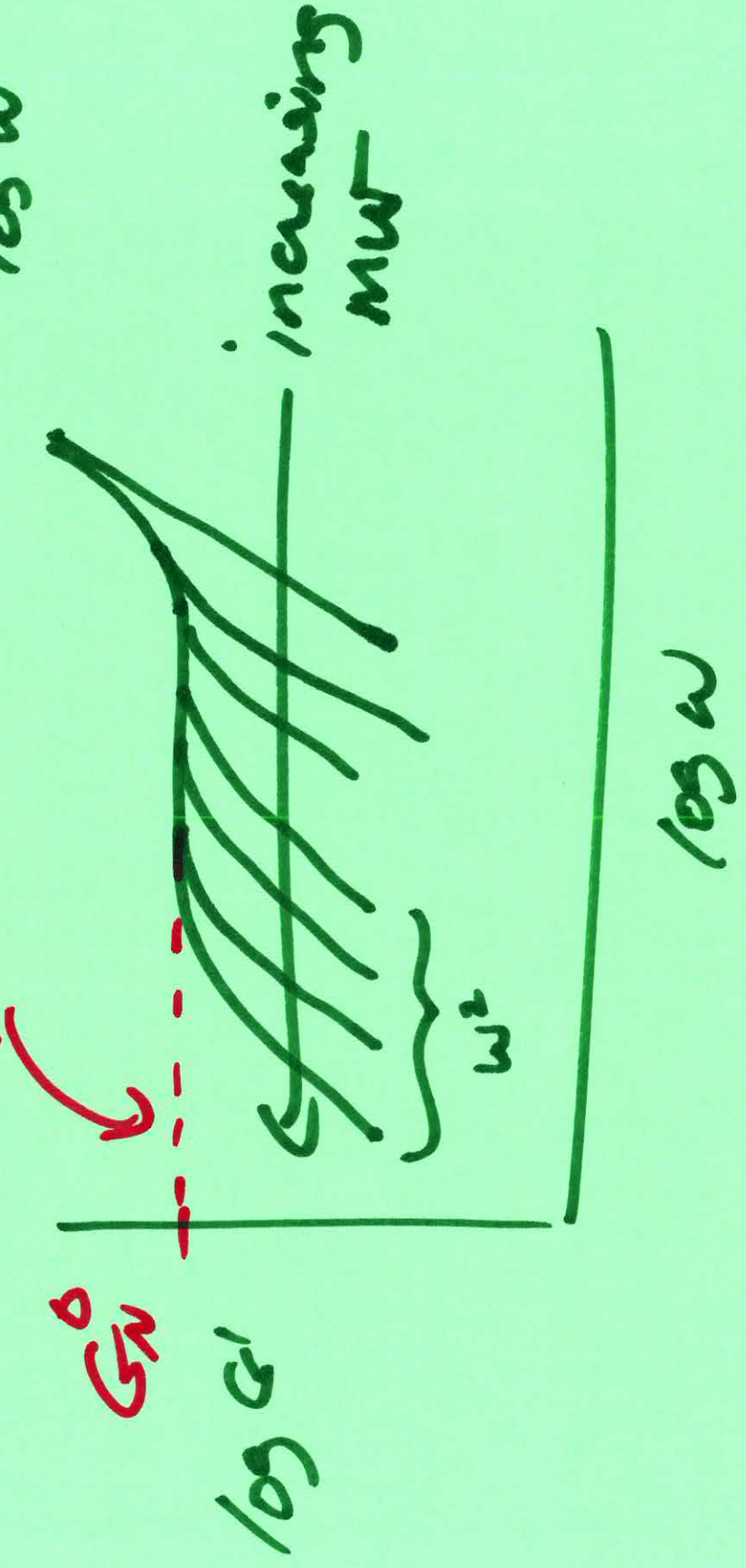


⑥



$\log \sigma$

(rubbery)
entanglement
plateau



$\log W$

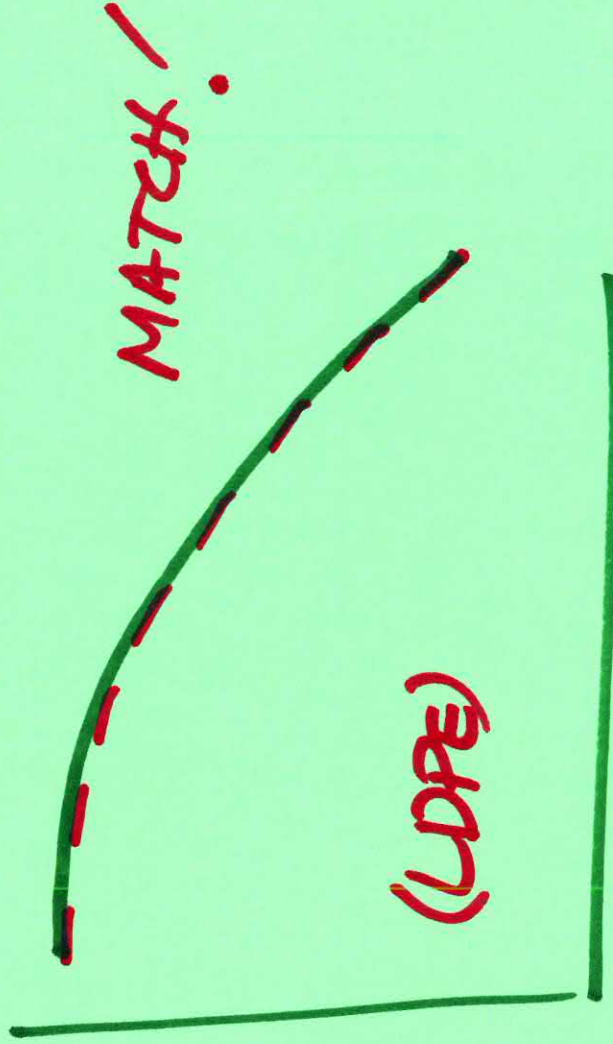
Cox-Merz
rule

(It only works
when it works.
matl w/ complex structures
do not follow Cox-Merz)

$\log \eta$
 $\log \eta^*$

$$\eta^* = \frac{\sqrt{G'{}^2 + G''{}^2}}{\omega}$$

Complex viscosity



$\log \dot{\gamma} \text{ (s}^{-1}\text{)}$
 $\log \omega \text{ (rad/s)}$

⑧

III Effect of Temperature on $\eta(\dot{\gamma})$ and SAOS

- time/temperature superposition allows "master curves" to be produced (with shift factors, a_T)
- works for $\eta(a_T \dot{\gamma})$
 $G'(a_T \omega), G''(a_T \omega)$

⑨

$$-\log a_T \propto \frac{1}{T(k)} \quad (\text{at high } T)$$

Arrhenius eqn

— empirical method to compactly represent data

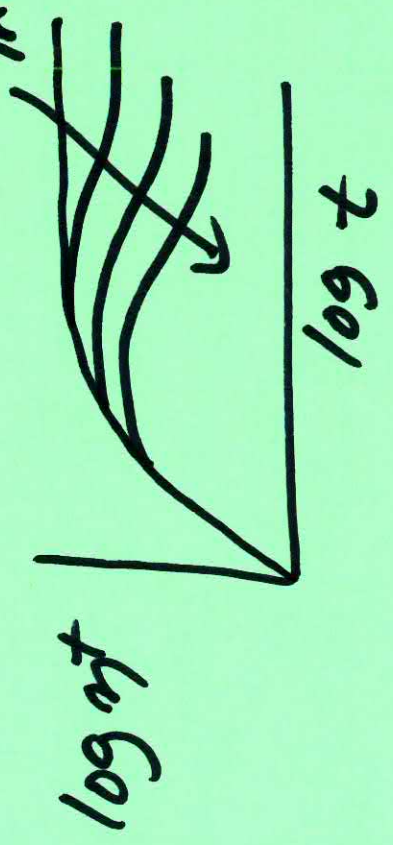
IV

Unsteady Shear

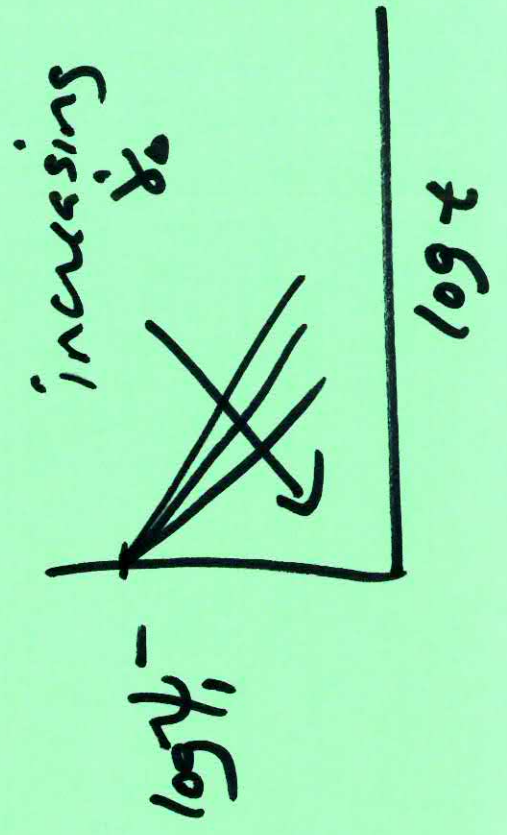
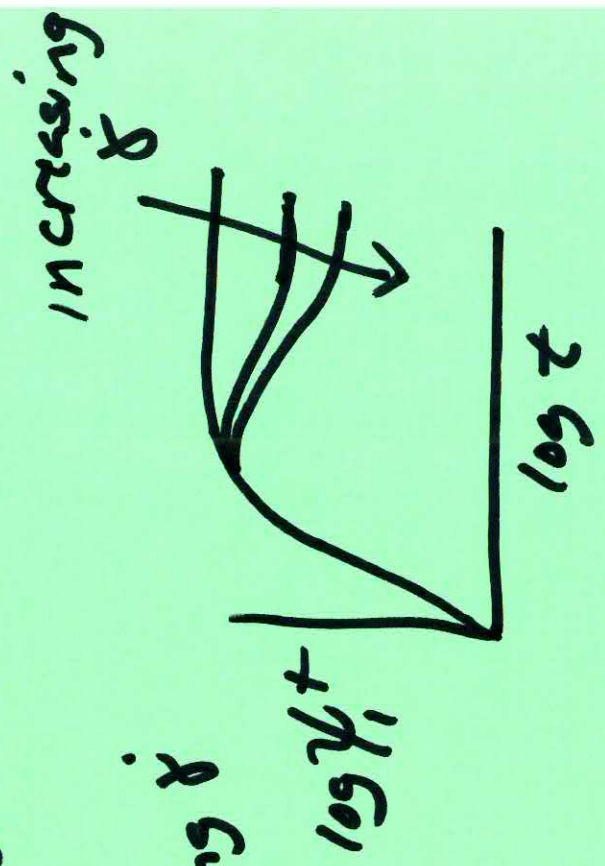
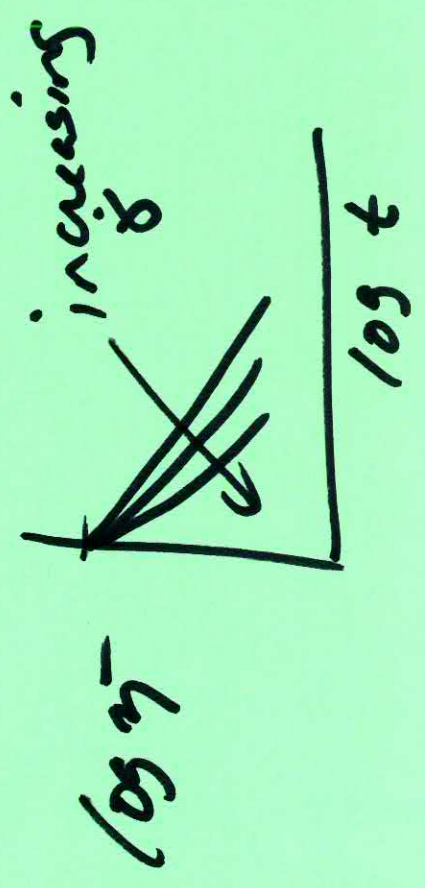
(large strain)

(10)

1. Start-up



2. Cessation



②

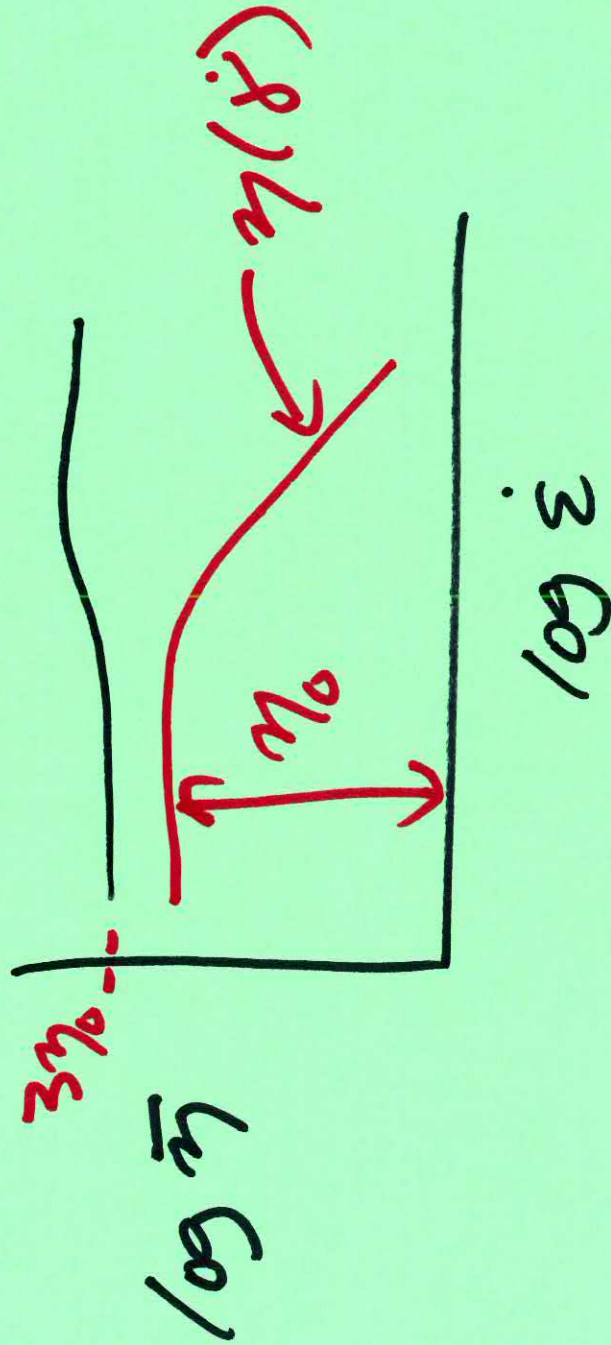
3. Step Strain

small strain limit



(12)

V Steady Elongation



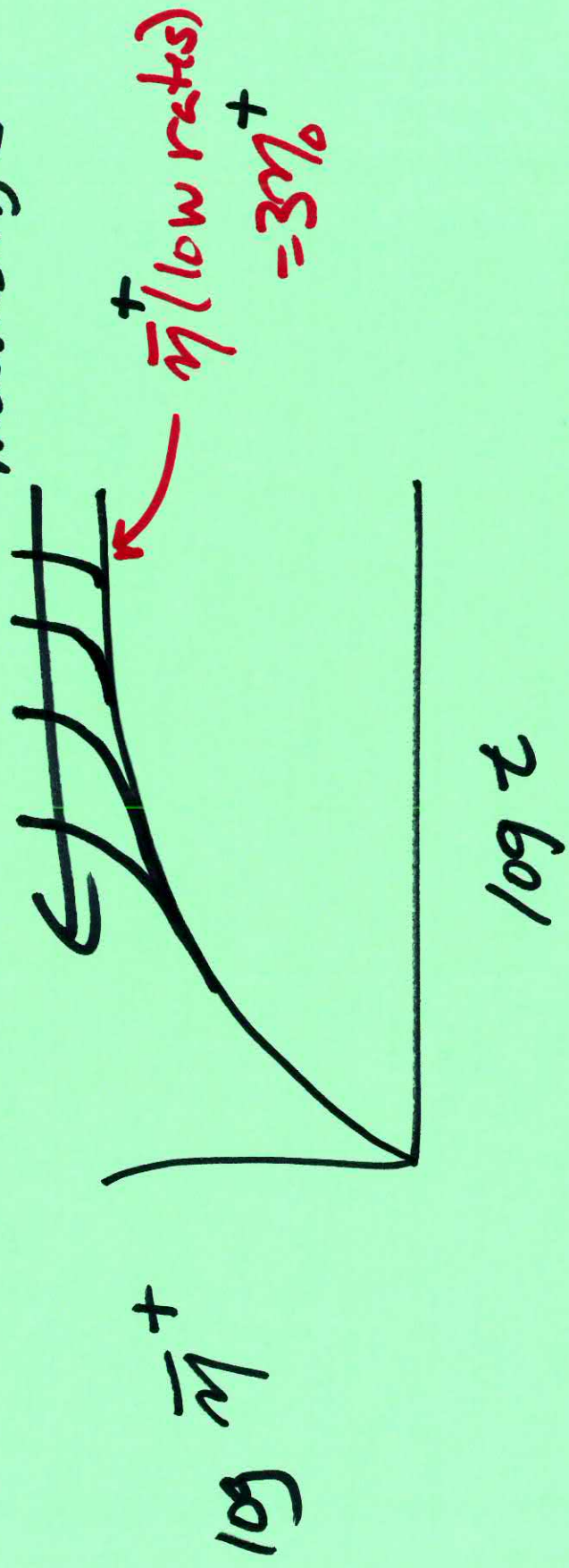
$$\text{Troun Ratio: } Tr \equiv \frac{\gamma(\dot{\epsilon})}{\dot{\gamma}(\dot{\epsilon})}$$

$$\lim_{\substack{\dot{\epsilon} \rightarrow 0 \\ \dot{\gamma} \rightarrow 0}} Tr = 3$$

13

VI Unsteady Elongation

increasing $\dot{\epsilon}$



Has a low rate "envelope" that is 3x the shear start-up result.

