

MIDTERM EXAM

CM3110

①

SOLUTION

21 OCT 2008

1. ERGUN EQN $\frac{150}{Re_p} + 1.75 = f_p$

2.

$$\rho = 1.000 \text{ g/cm}^3$$
$$\mu = 10^{-2} \text{ poise}$$



$$\rho_{\text{sphere}} = 1.050 \text{ g/cm}^3$$
$$D = 0.1002 \text{ cm}$$

$$v_s = 1.23 \times 10^{-2} \frac{\text{cm}}{\text{s}}$$

$C_D = ?$

calc Re : $Re = \frac{\rho v D}{\mu}$

$$= \frac{(1.000 \text{ g})}{\text{cm}^3} \left(\frac{1.23 \times 10^{-2} \text{ cm}}{\text{s}} \right) (0.1002 \text{ cm})$$

$$\boxed{Re = 0.1232} \quad \frac{10^{-2} \text{ g}}{\text{cm} \cdot \text{s}}$$

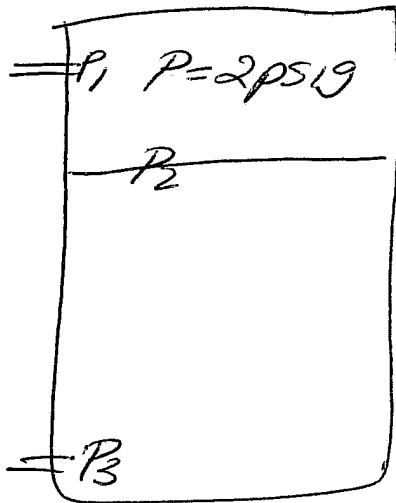
⇒ STOKES FLOW

⇒ $C_D = \frac{24}{Re}$

$C_D = \frac{24}{0.1232} = 194.805$

$C_D = 195$ 3 SIG FIGS //

3.



$P_1 = 2.00 \text{ psig}$
 $P_2 = 2.00 \text{ psig}$

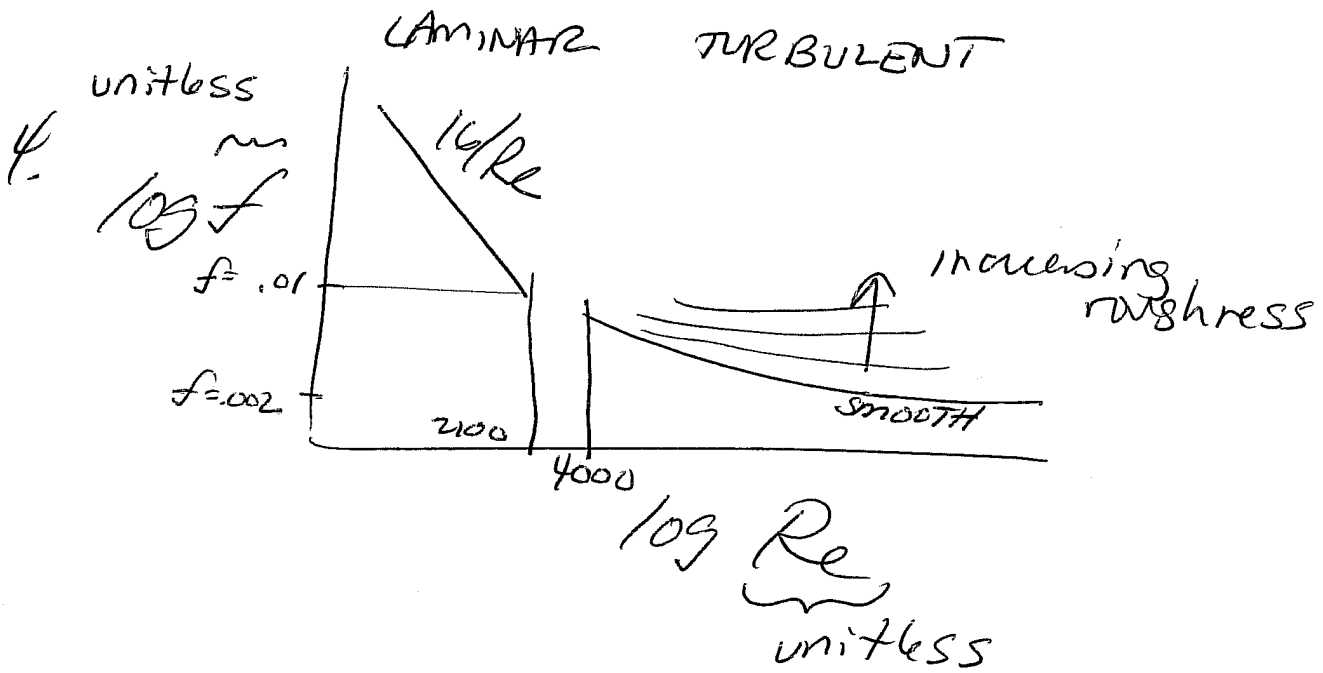
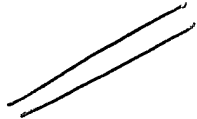
$P_3 = P_1 + \rho g H$

$= 2 \text{ psig} + \left(\frac{1.143 \text{ g}}{\text{cm}^3} \right) \left(\frac{980 \text{ cm}}{\text{s}^2} \right) \left(\frac{220 \times 10^2 \text{ cm}}{1} \right)$
 $\times \frac{1 \text{ dyne s}^2}{\text{g cm}} \frac{\text{cm}^2}{1.01325 \times 10^6 \text{ dynes}} 14.696 \text{ psi}$

$$P_3 = 2 \text{ psig} + 3.574 \text{ psi}$$

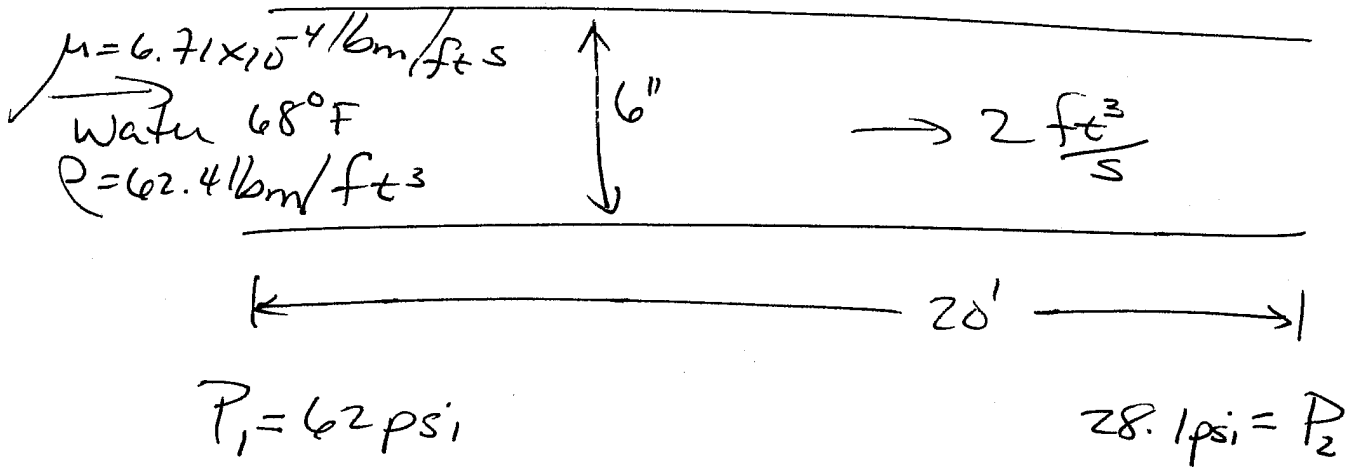
$$P_3 = 5.574 \text{ psig}$$

$$P_3 = 5.57 \text{ psig}$$



5.

(5)



(a) Total drag on walls

$$F_{\text{drag}} = \Delta P \frac{\pi D^2}{4}$$

$$= \frac{(62 - 28.1) \frac{\text{lb}_f}{\text{in}^2} (\pi) (6 \text{ in})^2}{4}$$

$$= 958.500 \text{ lb}_f$$

$$F_{\text{drag}} = 958 \text{ lb}_f$$

$$\langle V \rangle = \frac{Q}{A} = \left(\frac{2 \text{ ft}^3}{\text{s}} \right) \left(\frac{4}{\pi (0.5 \text{ ft})^2} \right) = 10.1859 \frac{\text{ft}}{\text{s}}$$

(6)

b. What is roughness factor ϵ ?

$$f = \frac{F_{\text{drag}}}{\left(\frac{1}{2} \rho V^2\right) (\pi DL)}$$

$$= \frac{(958.4999186 \frac{\text{lb}}{\text{ft}^3}) \frac{32.174 \text{ ft} \cdot \text{lbm}}{\text{lb} \cdot \text{s}^2}}{\frac{1}{2} \left(62.4 \frac{\text{lbm}}{\text{ft}^3}\right) \left(10.1859 \frac{\text{ft}}{\text{s}}\right)^2 \pi (0.5 \text{ ft})}$$

(20 ft)

$$f = 0.303$$

$$\Rightarrow \boxed{\epsilon \gg 0.04}$$

$f=0.30$

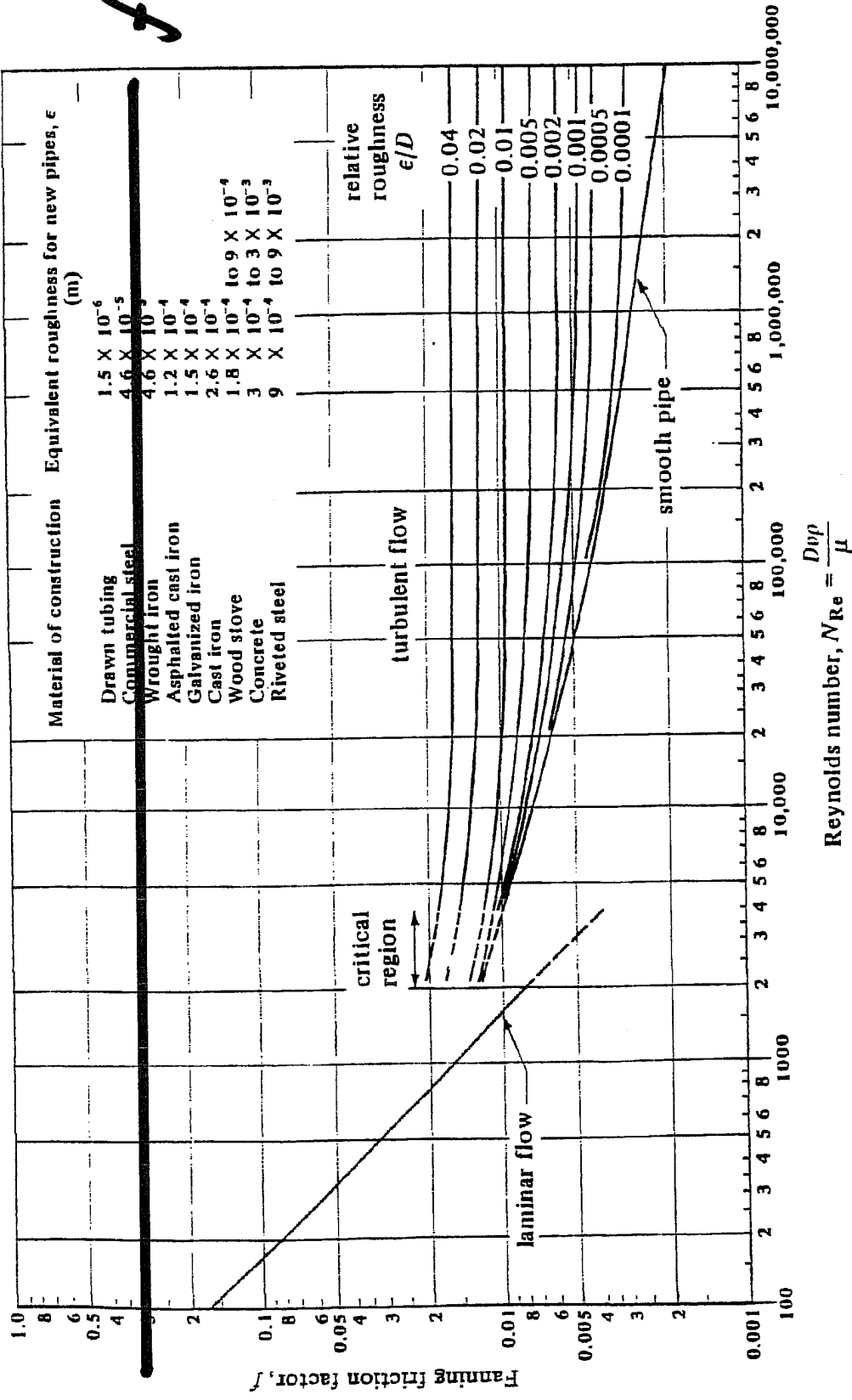


FIGURE 2.10-3. Friction factors for fluids inside pipes. [Based on L. F. Moody, *Trans. A.S.M.E.*, 66, 671 (1944); *Mech. Eng.* 69, 1005 (1947). With permission.]