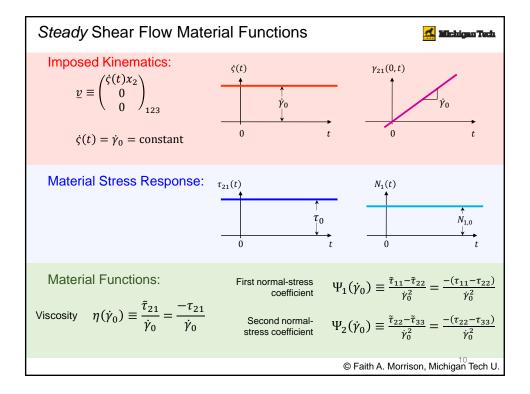
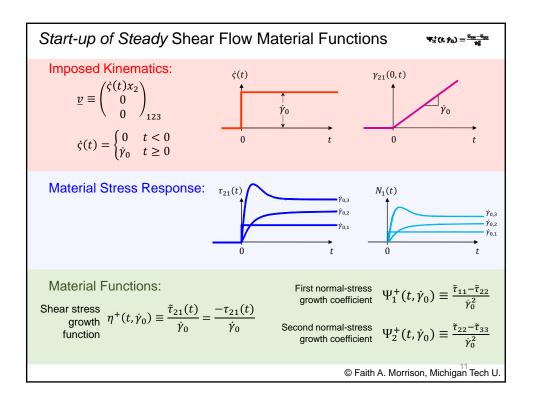


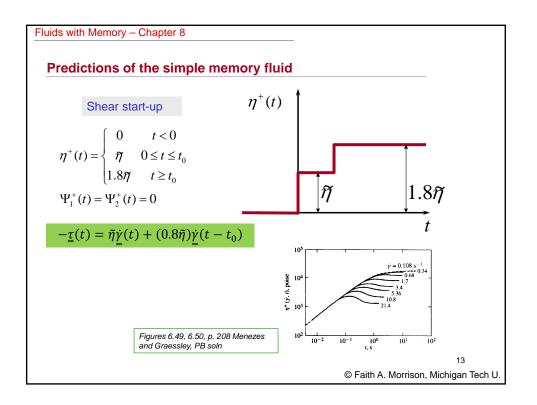
Fluids with Memory – Chapter	8
What does this	s model predict? Simple memory fluid $-\underline{\tau}(t) = \tilde{\eta} \underline{\dot{\gamma}}(t) + (0.8\tilde{\eta}) \underline{\dot{\gamma}}(t - t_0)$
Steady shear	$\eta = ?$ $\Psi_1 = ?$ $\Psi_2 = ?$
Shear start-up	$\eta^{+}(t) = ?$ $\Psi_{1}^{+}(t) = ?$ $\Psi_{2}^{+}(t) = ?$
	8 © Faith A. Morrison, Michigan Tech U.

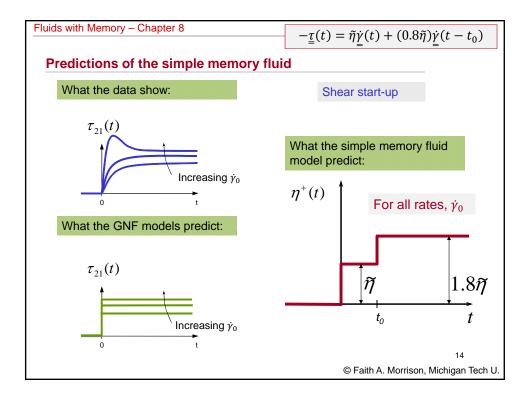
Fluids with Memory – Chapter a	8	
What does this	model predict? $-\underline{\underline{\tau}}(t) = \tilde{\eta}$	Simple memory fluid $\dot{\underline{\gamma}}(t) + (0.8\tilde{\eta})\dot{\underline{\gamma}}(t-t_0)$
Steady shear	$\eta = ?$ $\Psi_1 = ?$ $\Psi_2 = ?$	Let's try.
Shear start-up	$\eta^{+}(t) = ?$ $\Psi_{1}^{+}(t) = ?$ $\Psi_{2}^{+}(t) = ?$	
		9 © Faith A. Morrison, Michigan Tech U.

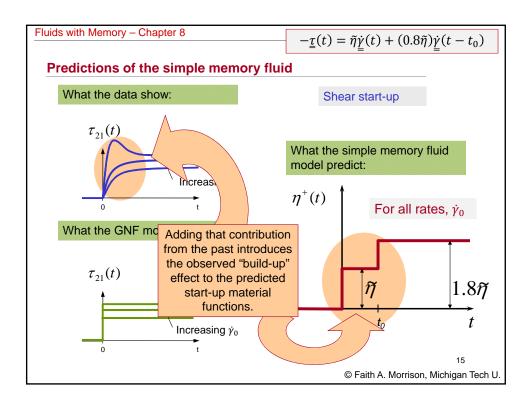


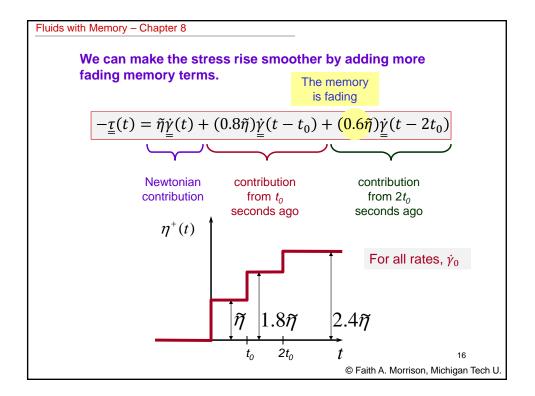


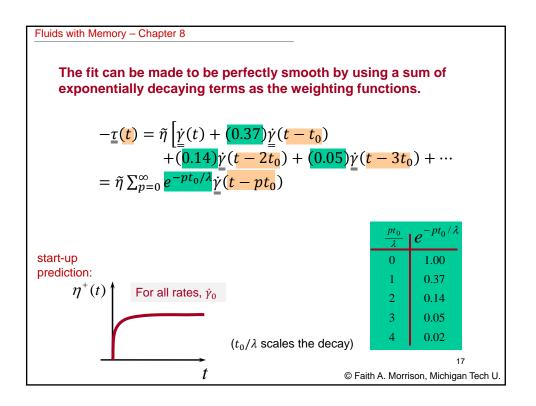
	$-\underline{\underline{\tau}}(t) =$	$= \tilde{\eta} \underline{\dot{\gamma}}(t) + (0.8\tilde{\eta}) \underline{\dot{\gamma}}(t - t_0)$
Steady shear	$\eta = 1.8\eta$ $\Psi_1 = \Psi_2 = 0$	The steady viscosity reflects contributions from what is currently happening and contributions from what happened t_0 seconds ago.
Shear start-up	(0	<i>t</i> < 0
	$\eta^+(t) = \begin{cases} 0\\ \eta\\ 1.8i \end{cases}$	$0 \le t \le t_0$
	1.81	$\tilde{j} \qquad t \ge t_0$
	$\Psi_{1}^{+}(t) = \Psi_{2}^{+}(t)$	(t) = 0

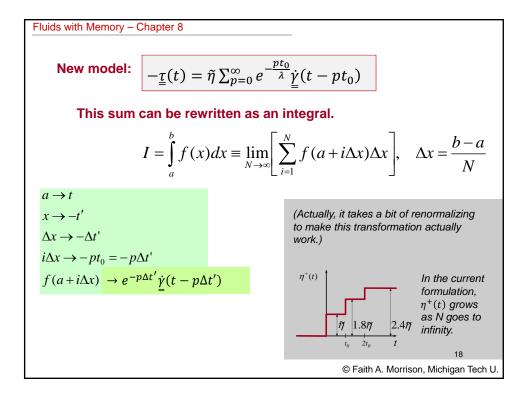


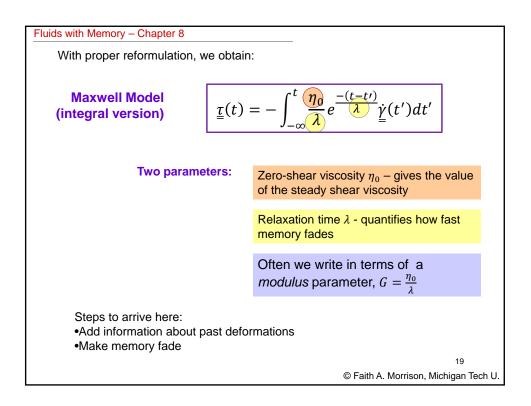


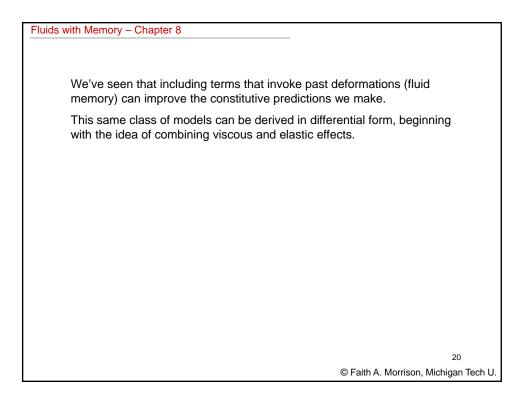


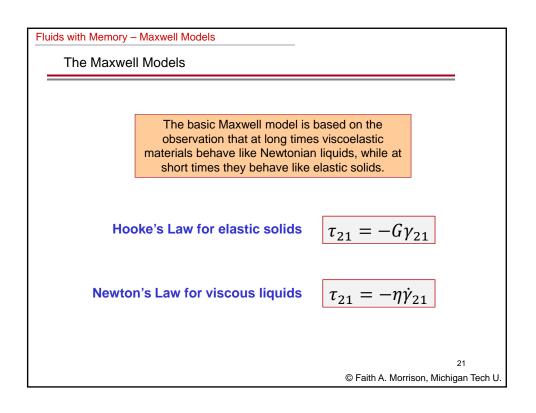


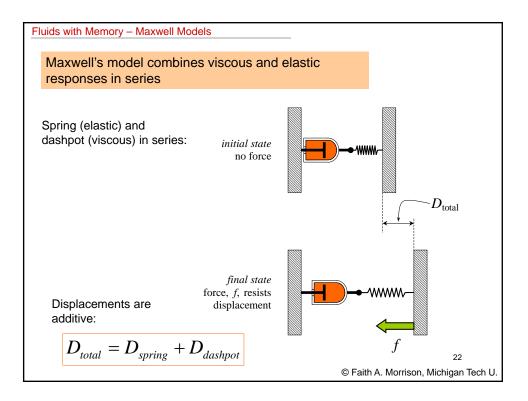


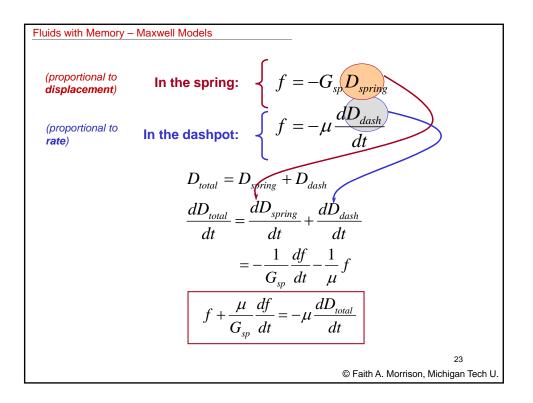


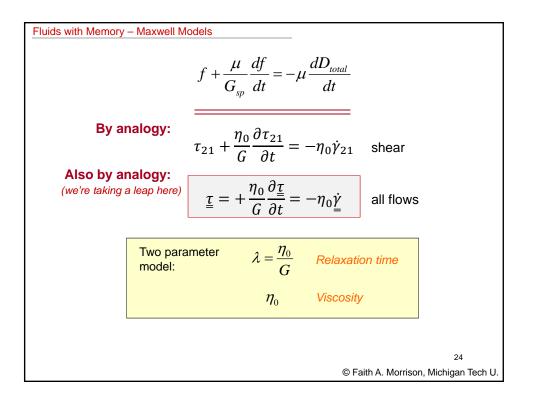


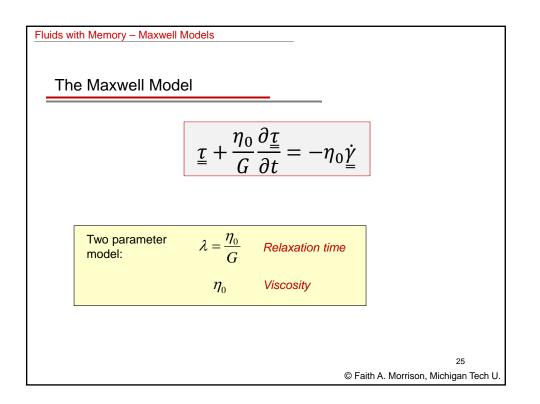


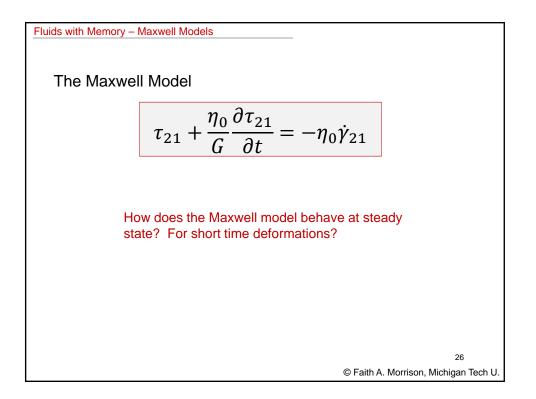


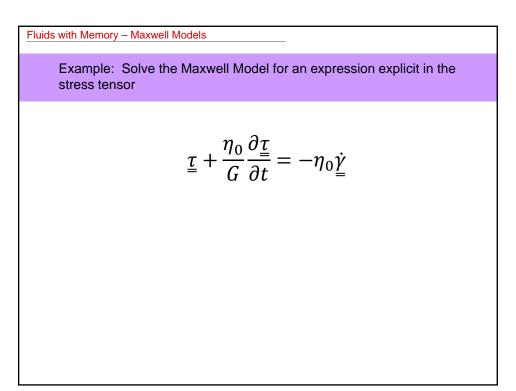


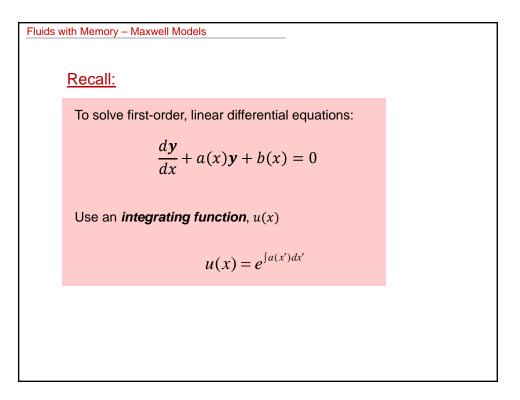


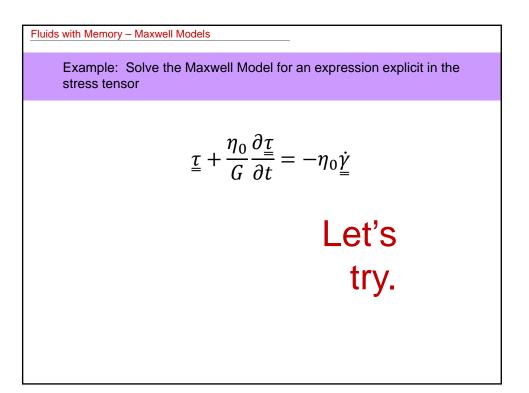


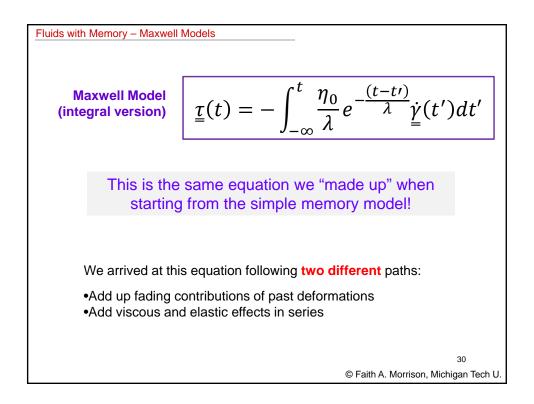


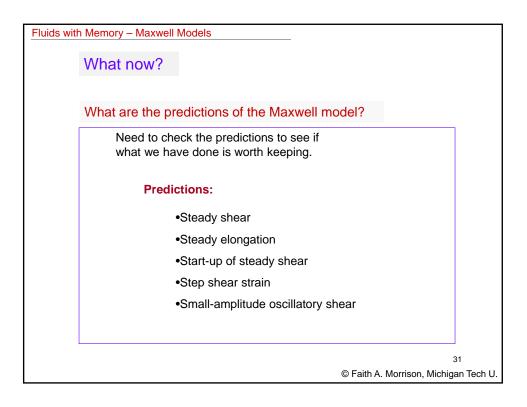


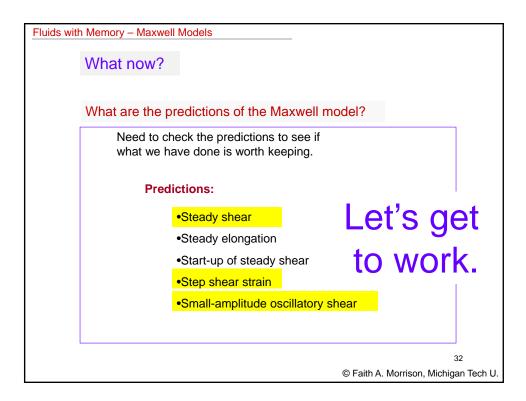


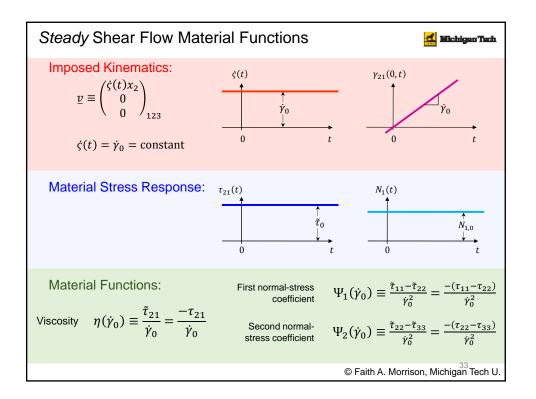


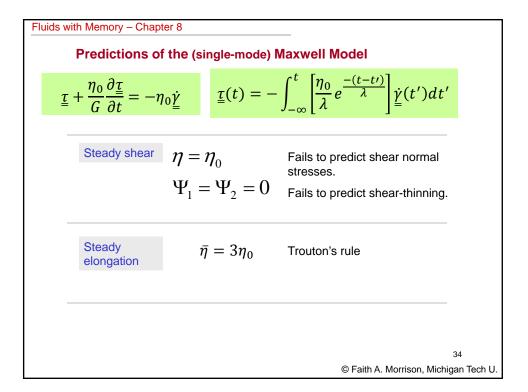


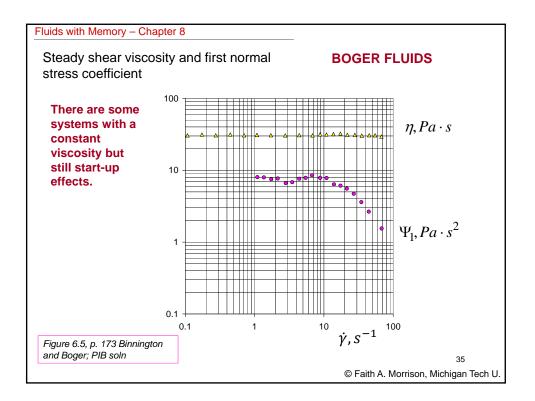


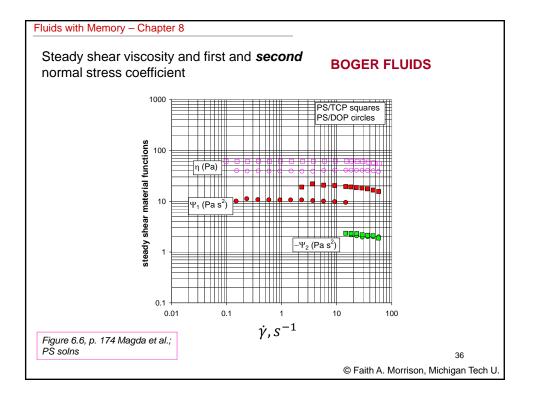


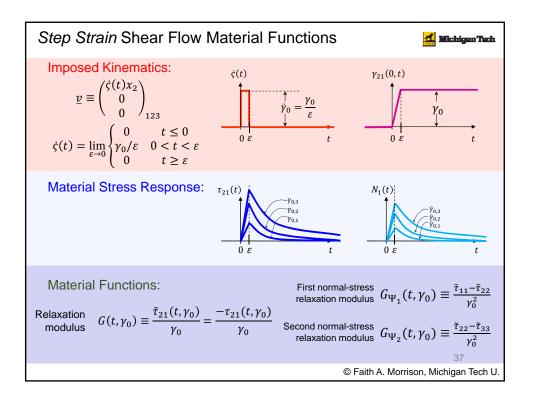


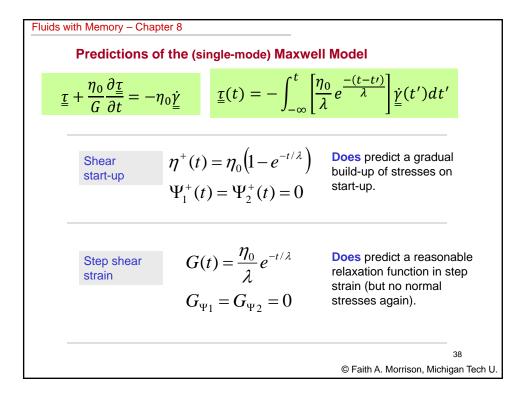


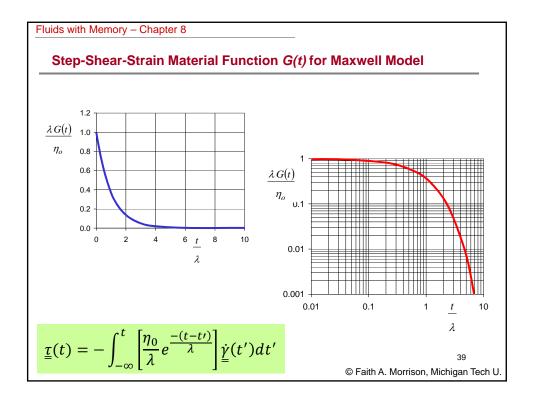


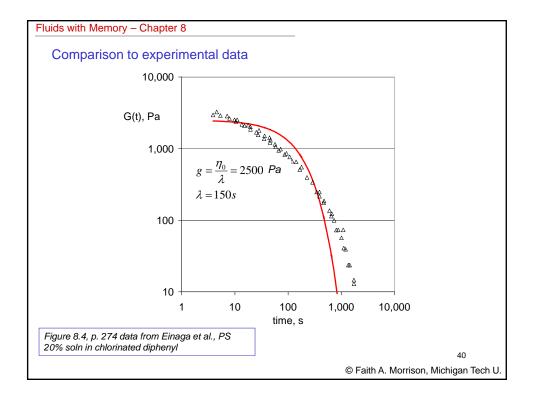


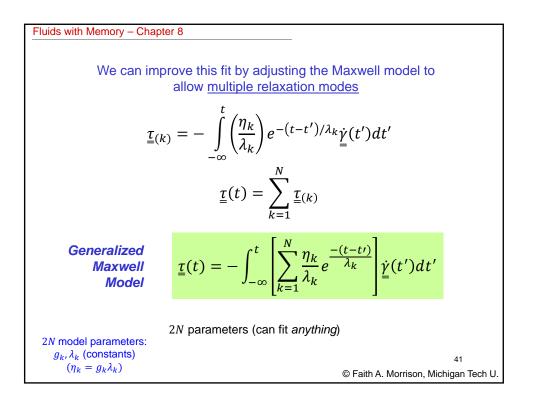


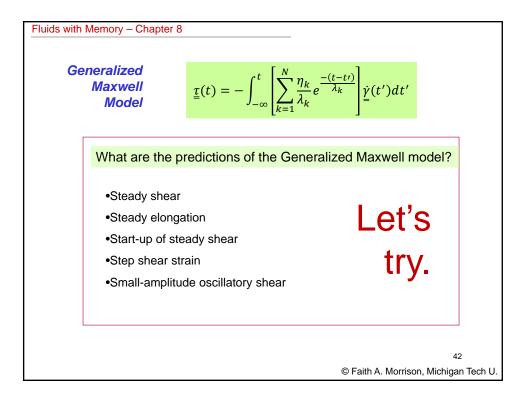


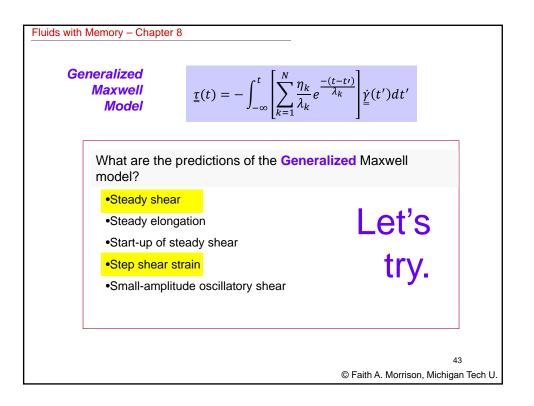


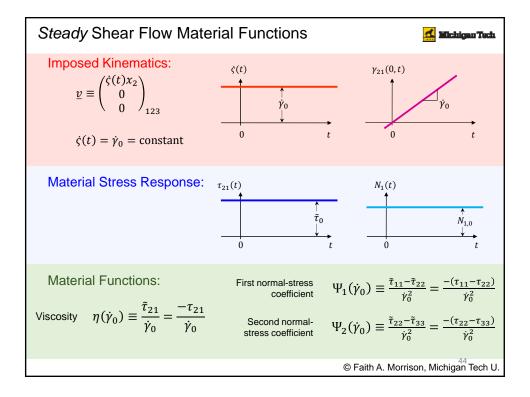


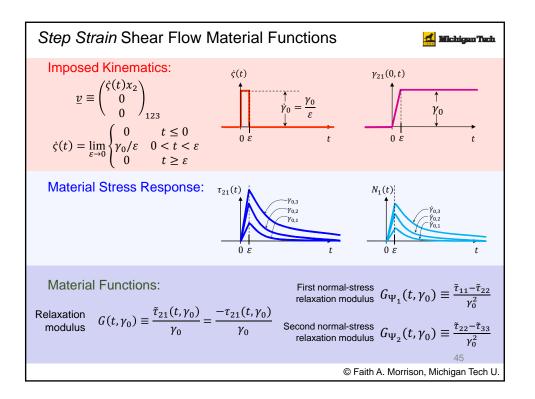












$2N \text{ model parame} \\ g_k, \lambda_k \text{ (constant} \\ (\eta_k = g_k \lambda_k)$	ters: s) $\underline{\underline{\tau}}(t) = -\int_{-\infty}^{t}$	$\left[\sum_{k=1}^{N} \frac{\eta_{k}}{\lambda_{k}} e^{\frac{-(t-t')}{\lambda_{k}}}\right] \underline{\dot{\gamma}}(t') dt'$
Steady shear	$\eta = \sum_{k=1}^{N} \eta_k$ $\Psi_1 = \Psi_2 = 0$	Fails to predict shear normal stresses Fails to predict shear- thinning
Step shear strain	$G(t) = \sum_{k=1}^{N} rac{\eta_k}{\lambda_k} e^{-t/\lambda_k}$	This function can fit <u>any</u> observed data (we show how)
	$G_{\Psi_1} = G_{\Psi_2} = 0$	Note that the GMM does no predict shear normal stresses.

