

**CM3310**  
**Exam 2**  
**March 18, 2004**  
**Open book/Open Notes**

Name: \_\_\_\_\_ Box No. \_\_\_\_\_

1. (25 pts) Given the block diagram in Figure 1, obtain the equivalent transfer function of  $T_{set}$  to  $T$ .

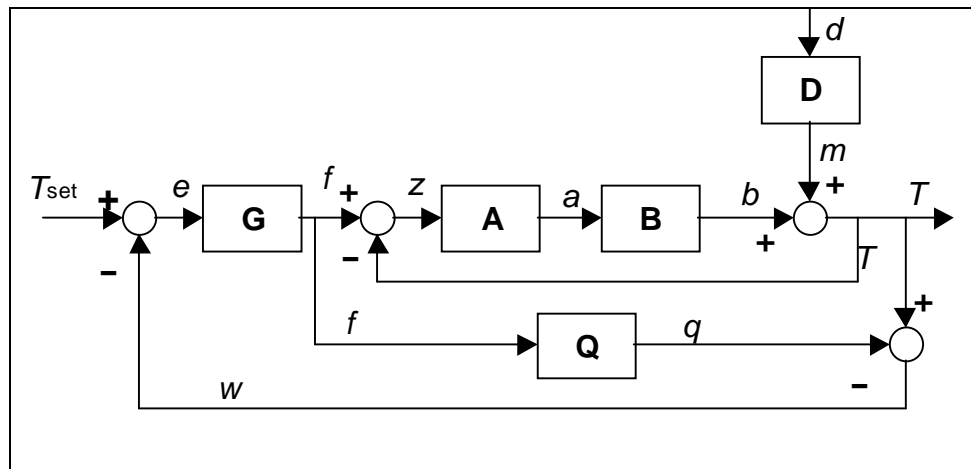


Figure 1.

(Hint: the transfer function from  $d$  to  $T$  is :  $\frac{D(1-GQ)}{GAB + (1+AB)(1-GQ)}$  )

2. (25 pts) A set of reactions are described by the following equations:

$$\frac{dC_A}{dt} = -(k_{AB} + k_{AC})C_A + k_{BA}C_B$$

$$\frac{dC_B}{dt} = k_{AB}C_A - k_{BA}C_B + C_{Bin}$$

where  $C_A$  and  $C_B$  are concentrations of A and B, while  $C_{Bin}$  is the concentrations of B in the feed. Obtain the transfer functions from  $C_{Bin}$  to  $C_A$ , assuming zero initial conditions (e.g. all concentrations are perturbed variables). The constants are  $k_{AB}=0.2$ ,  $k_{BA}=0.7$ ,  $k_{AC}=0.3$ .

3. (25 pts) For the block diagram shown in Figure 2, determine the range of values of  $K_c$  for which the system is stable.

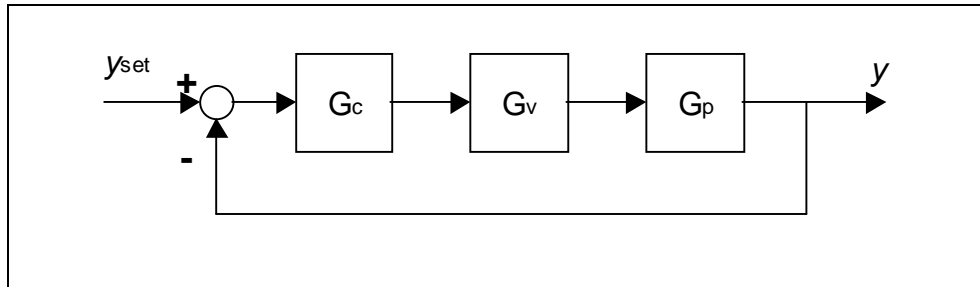


Figure 2.

where,

$$G_c = K_c \left( \frac{2s+1}{s+1} \right)$$

$$G_v = 2 \frac{1}{s+1}$$

$$G_p = \frac{-2s+1}{(3s+1)}$$

4. (25 pts) For the control system given in Figure 3, design a PI controller for  $G_c$  using the Ziegler-Nichols tuning rules.

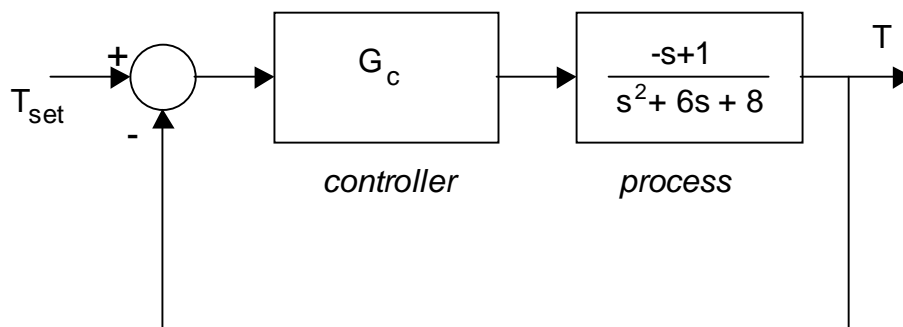


Figure 3.

5. Bonus (10pts): If one used a proportional controller with gain,  $K_c = 4$ , in the control system in Figure 3, determine the value of the steady state error for  $T_{set} = 50$ .